

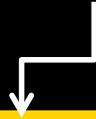
# The formation of cosmic structure

*Carlos S. Frenk*  
*Institute for Computational Cosmology,*  
*Durham*





cold dark matter



$\Lambda$ CDM: the standard model of  
cosmology



cosmological constant

Why is this the standard model?  
New tests and possible problems

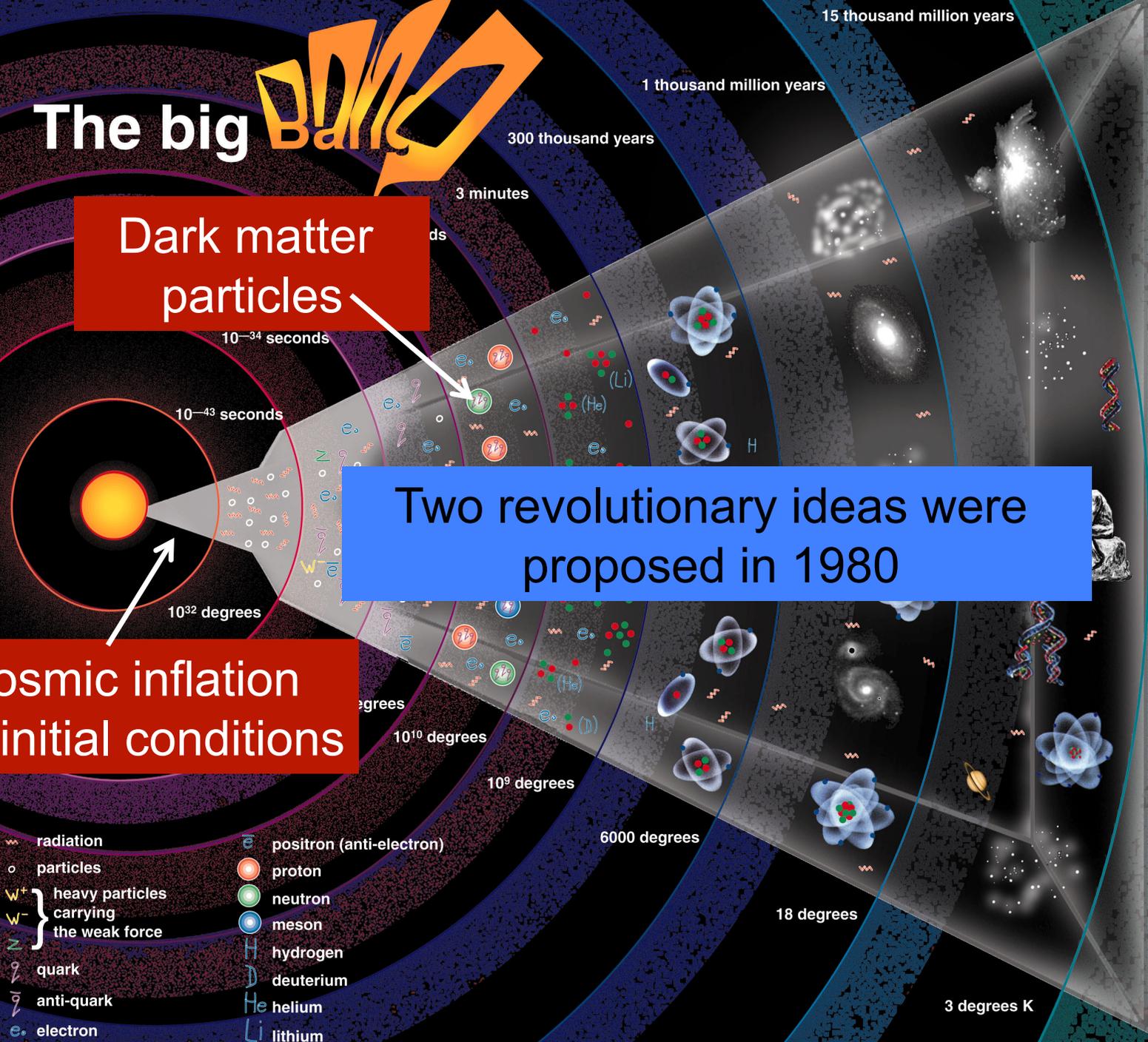
# The big Bang

Dark matter particles

Two revolutionary ideas were proposed in 1980

Cosmic inflation  
→ initial conditions

- radiation
- particles
- $W^+$  heavy particles carrying the weak force
- $W^-$
- quark
- anti-quark
- electron
- positron (anti-electron)
- proton
- neutron
- meson
- hydrogen
- deuterium
- helium
- lithium



# Non-baryonic dark matter candidates

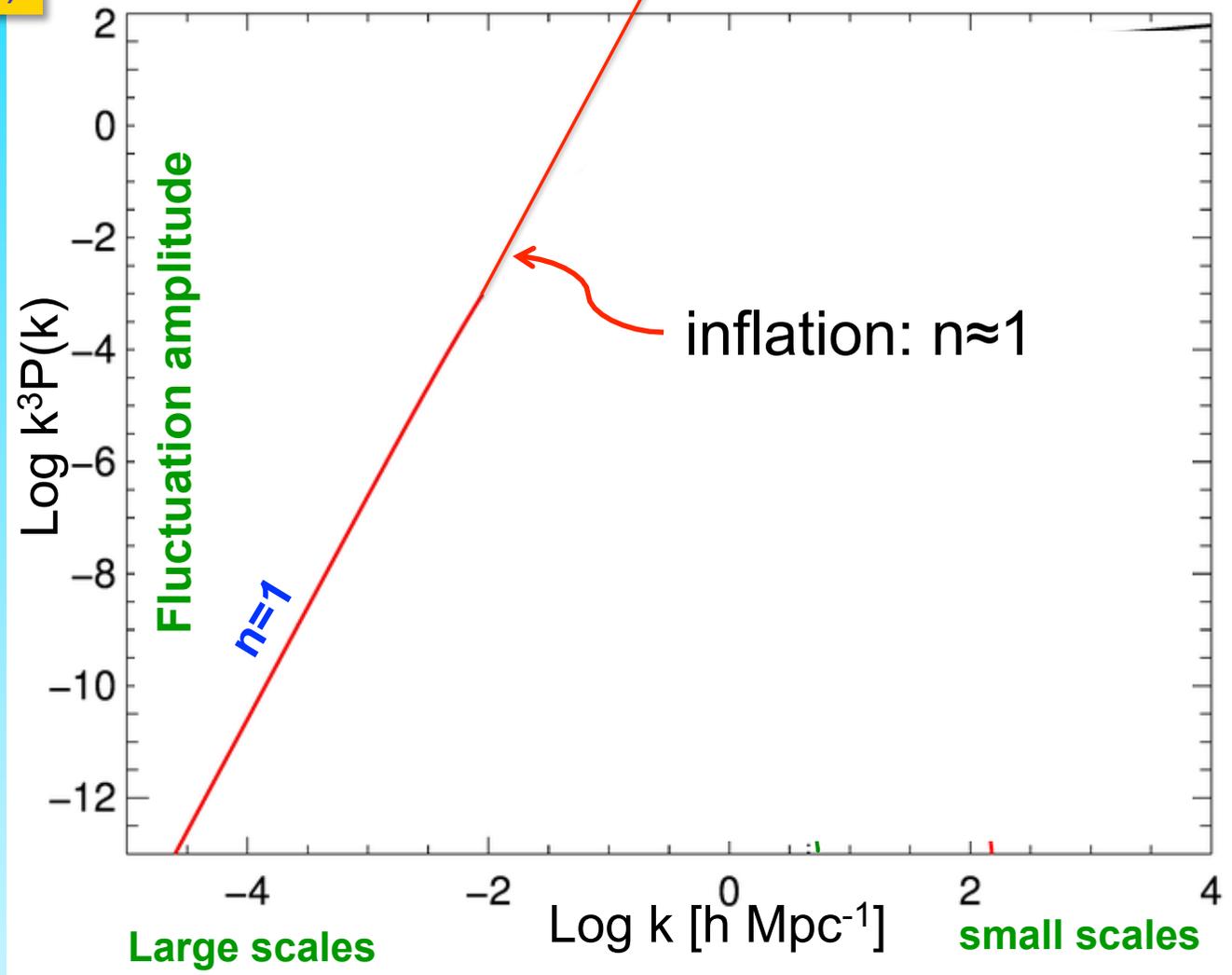
Type	example	mass
hot	neutrino	a few eV
warm	sterile $\nu$ majoron; KeVin	keV-MeV
cold	axion neutralino	$10^{-5}$ eV- >100 GeV

# The dark matter power spectrum

$k^3 P(k)$

The linear power spectrum (“power per octave”)

Prediction from inflation



# The dark matter power spectrum

$k^3 P(k)$

The linear power spectrum (“power per octave”)

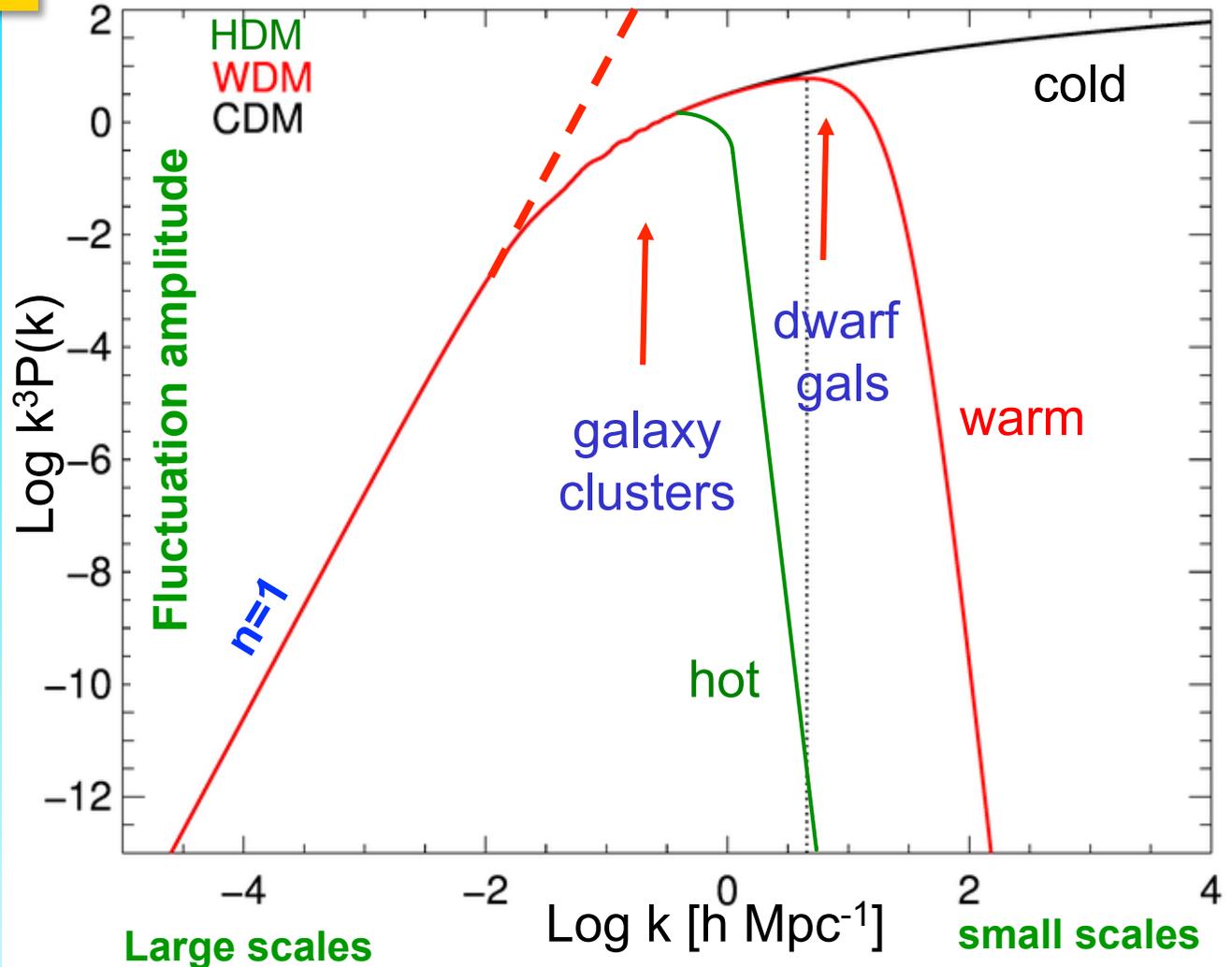
Free streaming →

$\lambda_{\text{cut}} \propto m_x^{-1}$   
for thermal relic

$m_{\text{CDM}} \sim 100\text{GeV}$   
susy;  $M_{\text{cut}} \sim 10^{-6} M_{\odot}$

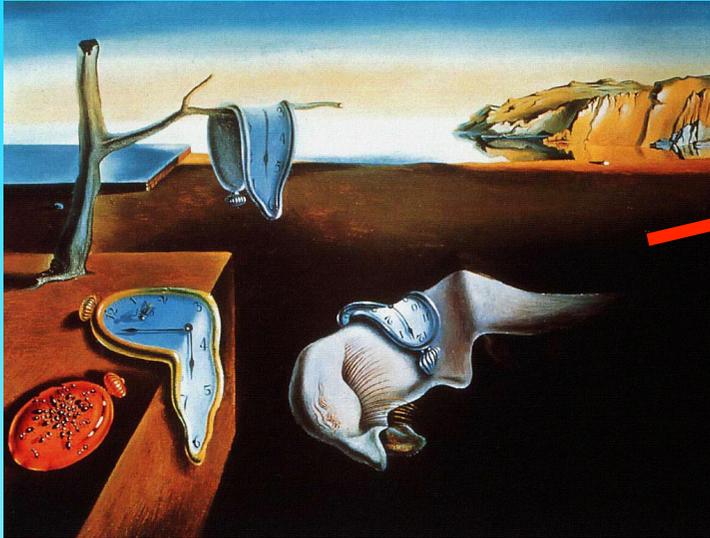
$m_{\text{WDM}} \sim \text{few keV}$   
sterile  $\nu$ ;  $M_{\text{cut}} \sim 10^9 M_{\odot}$

$m_{\text{HDM}} \sim \text{few eV}$   
light  $\nu$ ;  $M_{\text{cut}} \sim 10^{15} M_{\odot}$



# The formation of cosmic structure

$t=10^{-35}$  seconds



“Cosmology machine”



$t=380,000$  yrs

$\delta\rho/\rho \sim 10^{-5}$

Simulations

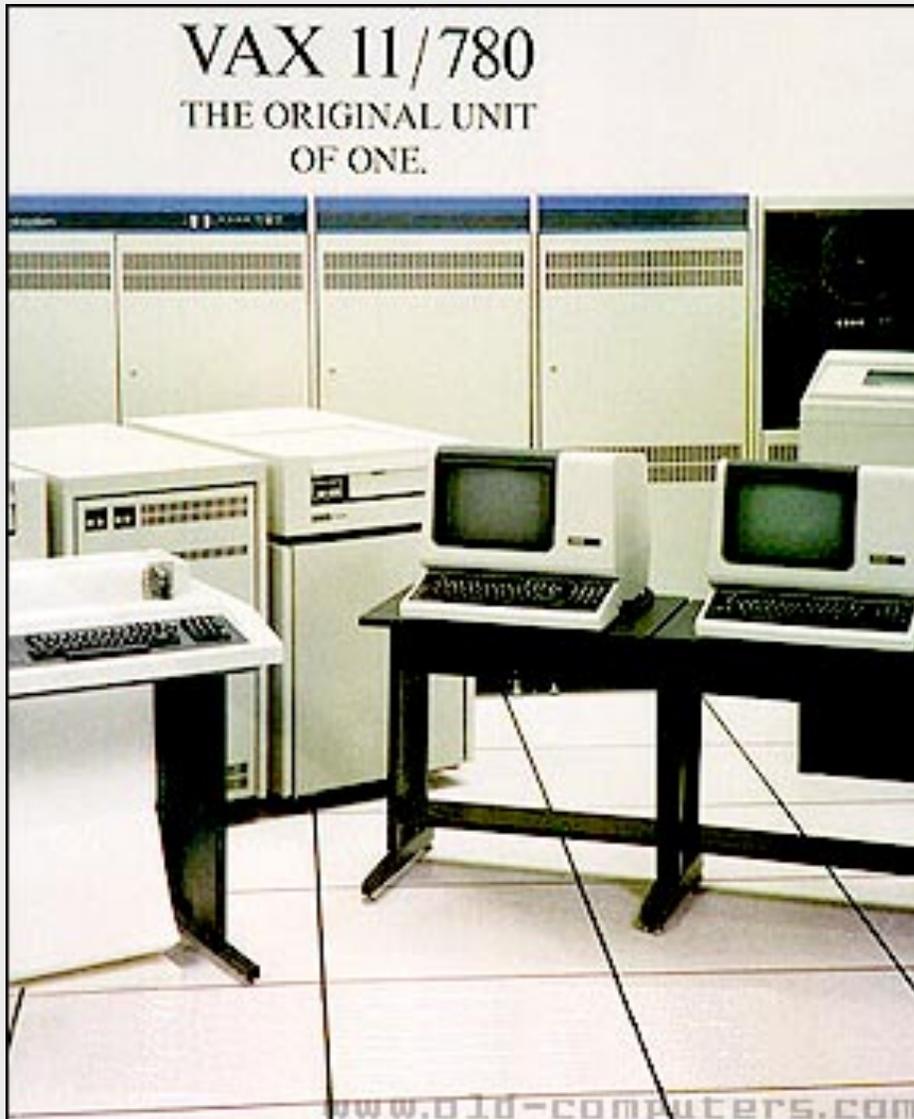
Supercomputer **simulations** are the best technique for calculating how small **primordial perturbations** grow into **galaxies** today



$t=13.8$  billion yrs

$\delta\rho/\rho \sim 1-10^6$

# The universe in a computer

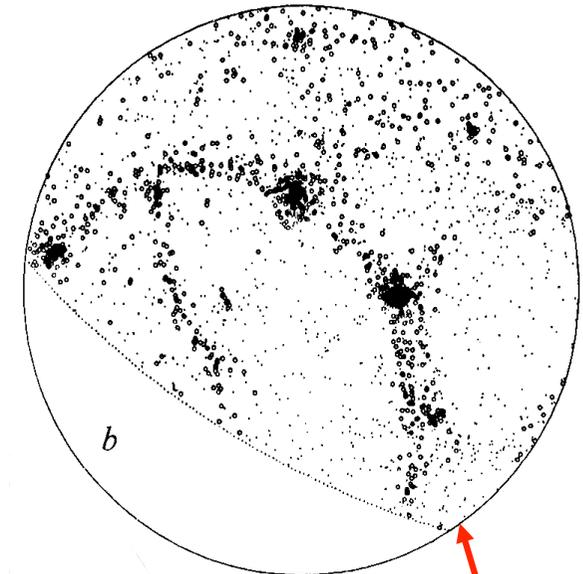


December 1981

Speed = 500,000 FLOPS

RAM = 4 Mbytes

# Non-baryonic dark matter cosmologies



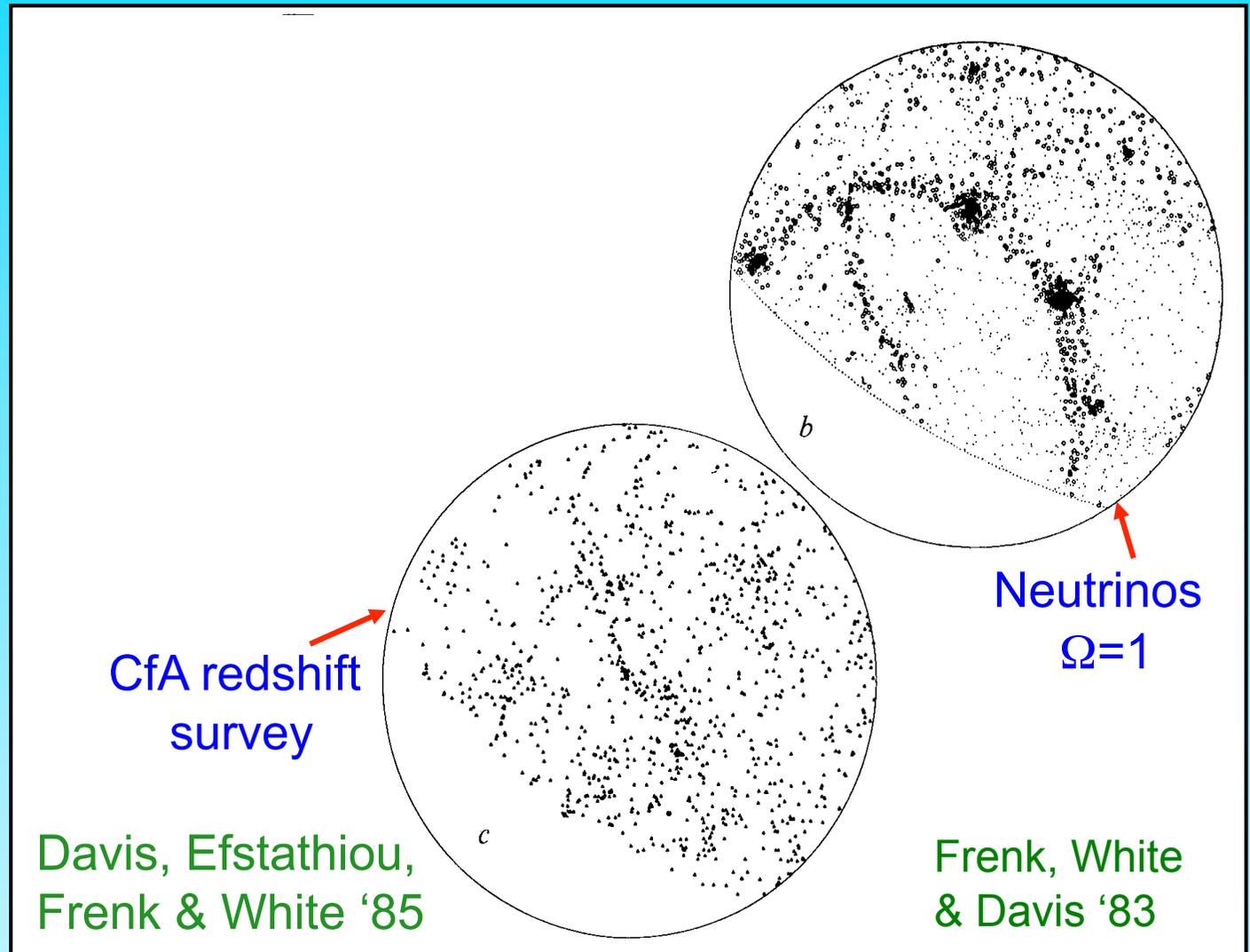
Neutrinos  
 $\Omega=1$

Frenk, White  
& Davis '83

# Non-baryonic dark matter cosmologies

Neutrino DM  $\rightarrow$   
unrealistic clust'ing

Neutrinos cannot  
make appreciable  
contribution to  $\Omega$   
 $\rightarrow m_\nu \ll 10 \text{ eV}$



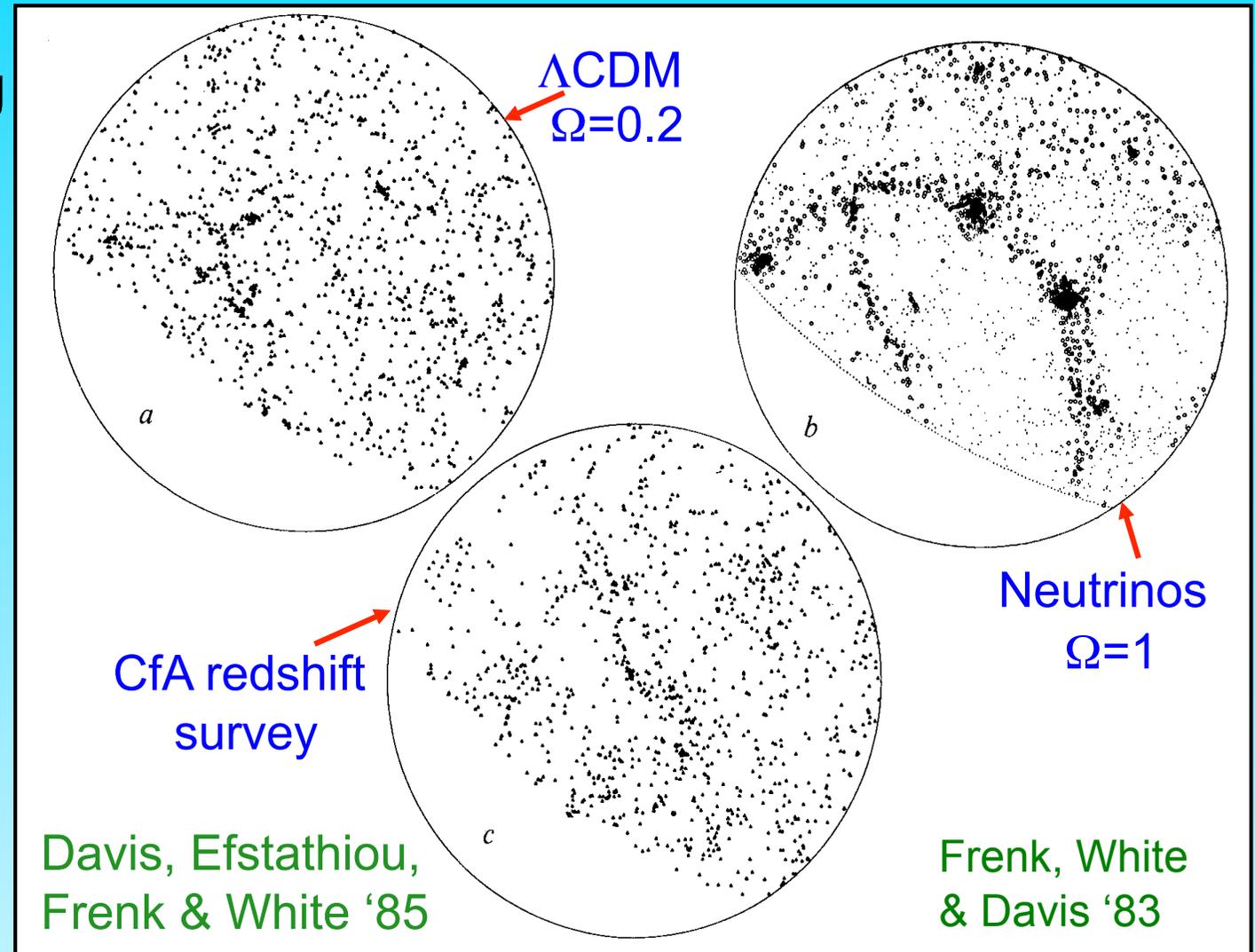
# Non-baryonic dark matter cosmologies

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unrealistic clust'ing

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make appreciable  
contribution to  $\Omega$   
 $\rightarrow m_\nu \ll 10 \text{ eV}$

Early CDM N-body  
simulations gave  
promising results

In CDM structure  
forms hierarchically



# Non-baryonic dark matter candidates

Type                      example                      mass

<del>hot</del>	<del>neutrino</del>	<del>a few eV</del>
warm	sterile $\nu$ majoron	keV-MeV
 cold	axion neutralino	$10^{-5}$ eV- >100 GeV



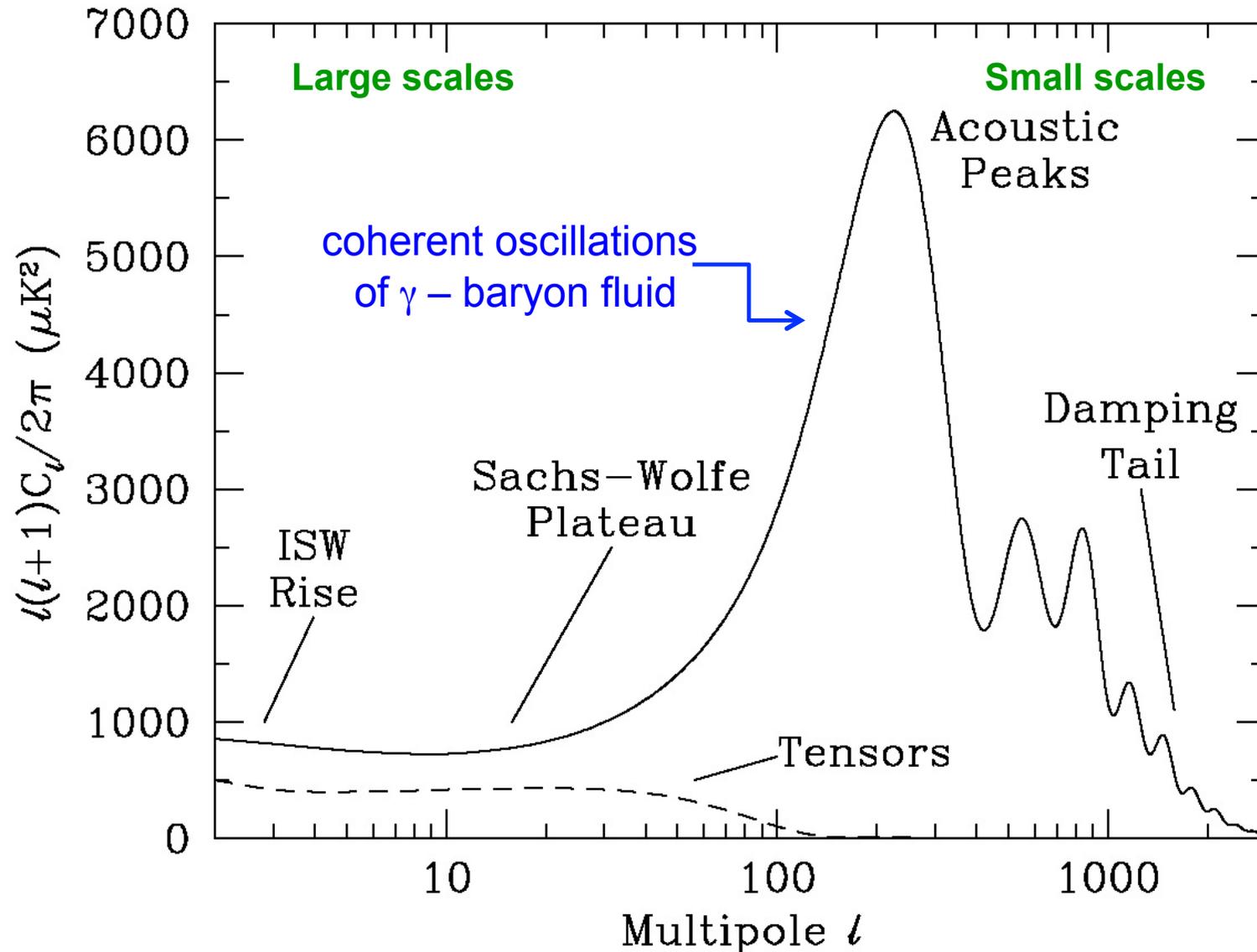
$\Lambda$ CDM model is an *a priori*  
implausible model!

... but makes definite predictions and is therefore testable

Main successes of the CDM cosmogony:

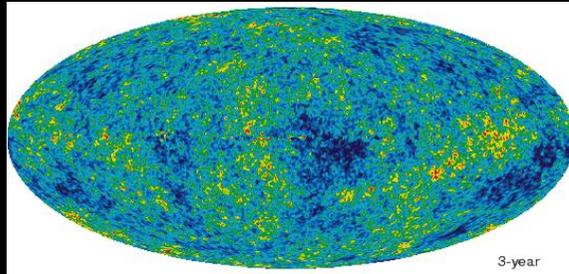
1. CMB temp. anisotropies: predicted in 1981, discovered in 1993
2. Spatial distribution of gals (1990- QDOT, APM, 2dFGRS, SDSS)
3. General features of galaxy luminosity function (1991 - )
4. Evolution of the galaxy population (2000 - )

# Temperature anisotropies in CMB



After Peebles & Yu '70; Peebles '82

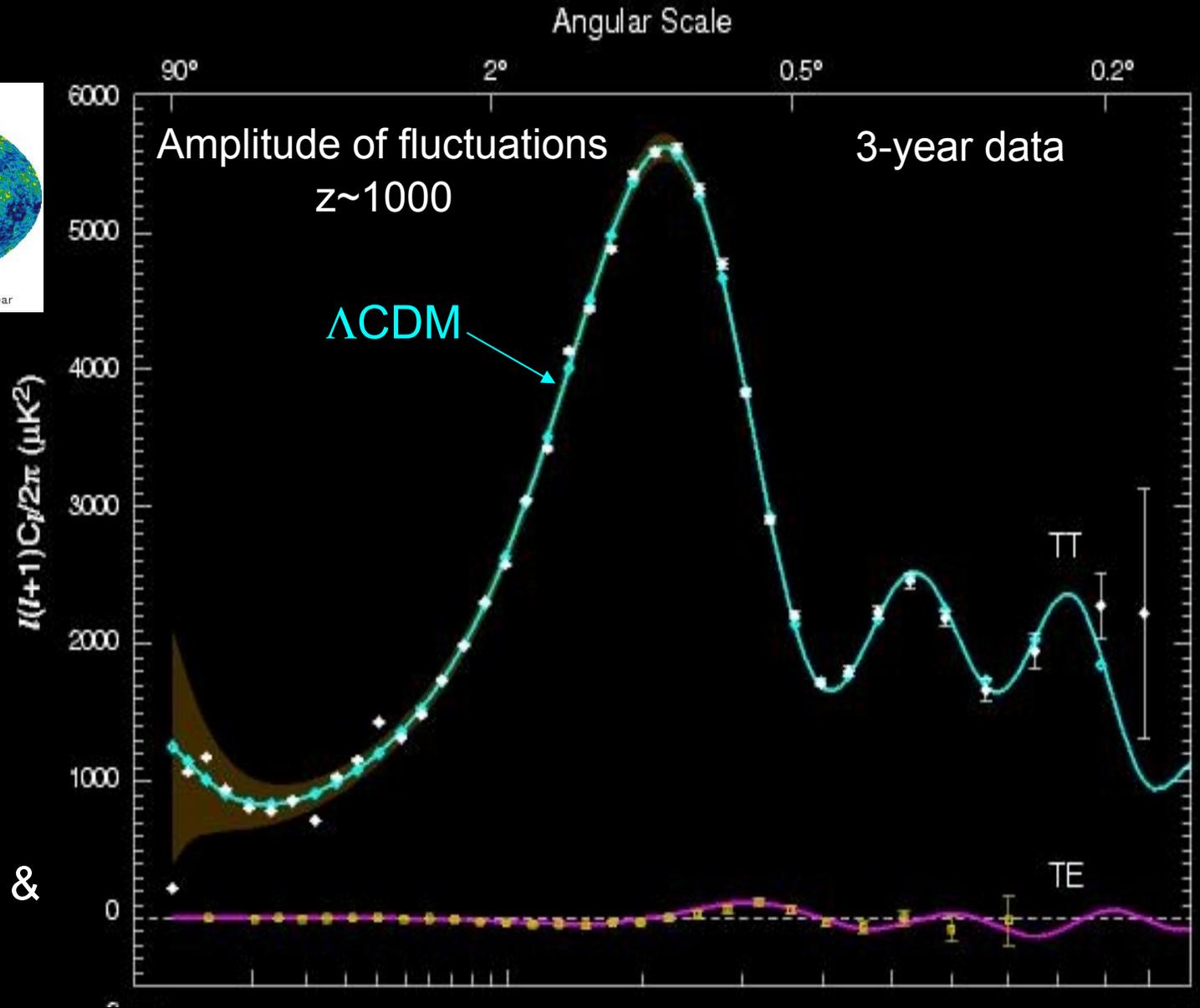
# WMAP temp anisotropies in CMB



The data confirm  
the theoretical  
predictions  
(linear theory)

Peebles '82; Bond &  
Efstathiou '80s

Hinshaw et al '06



Main successes of the CDM cosmogony:

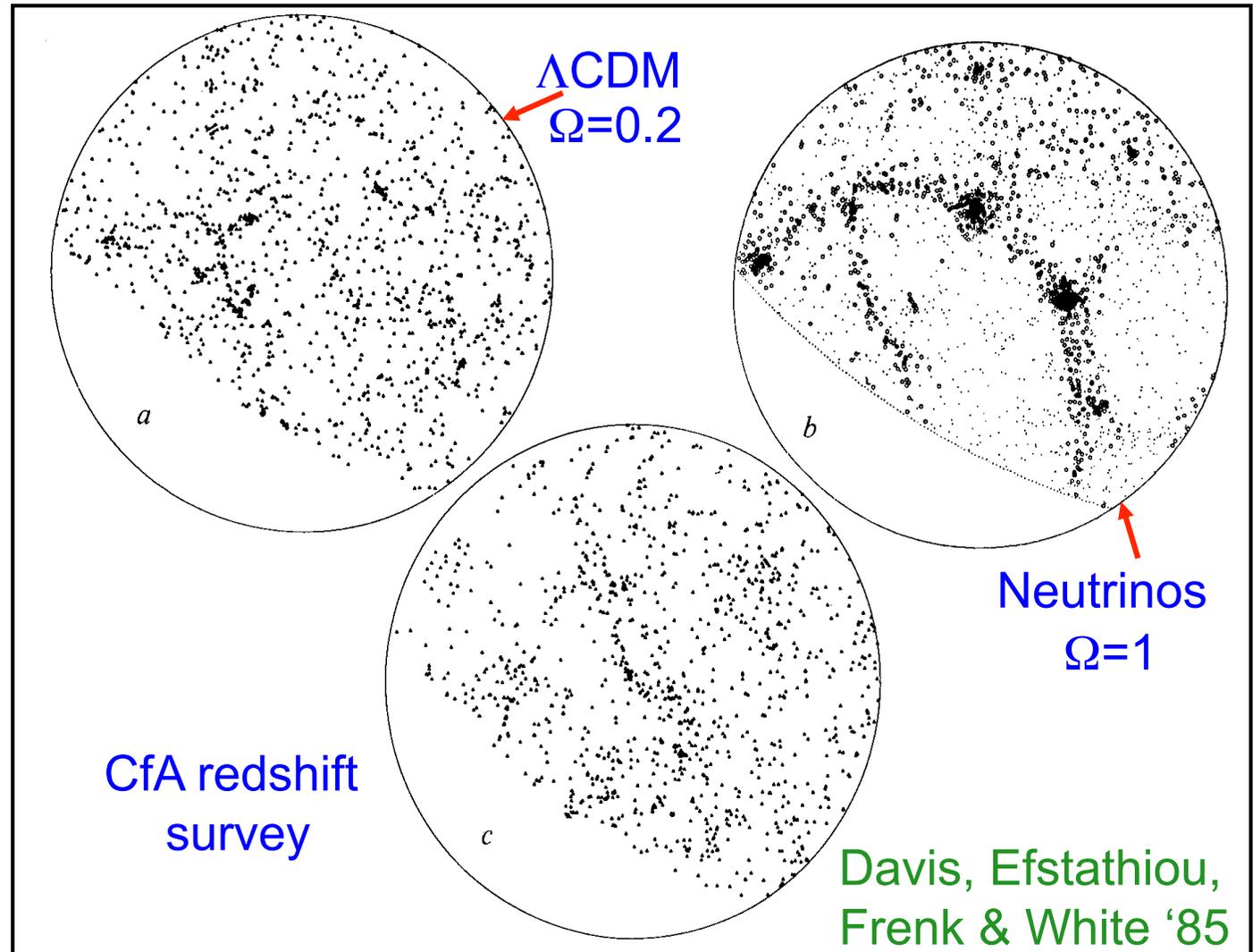
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# Non-baryonic dark matter cosmologies

Neutrino dark matter produces unrealistic clustering

Early CDM N-body simulations gave promising results

In CDM structure forms hierarchically



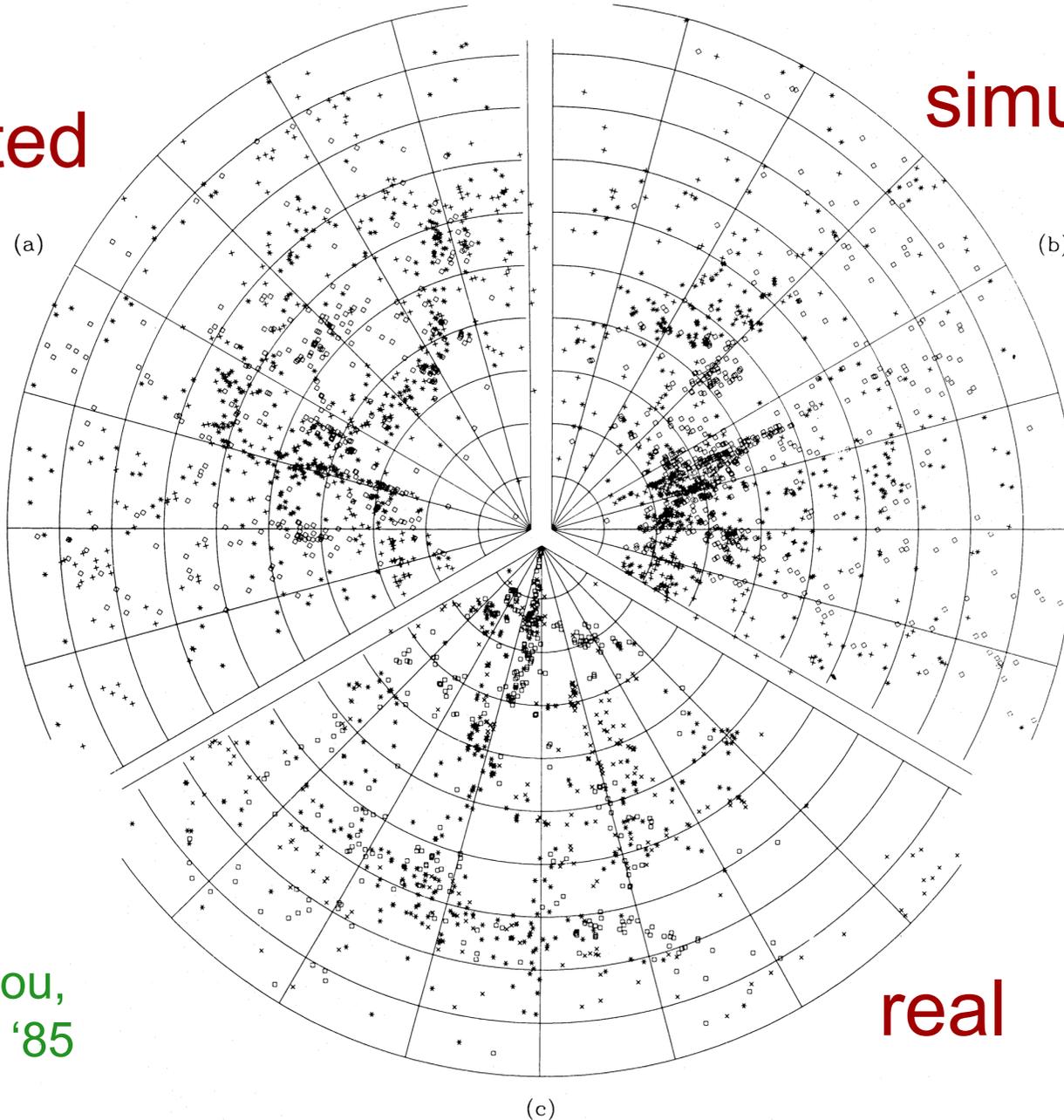


University of Durham

# Early simulations of $\Lambda$ CDM

simulated

simulated



Davis, Efstathiou,  
Frenk & White '85

real

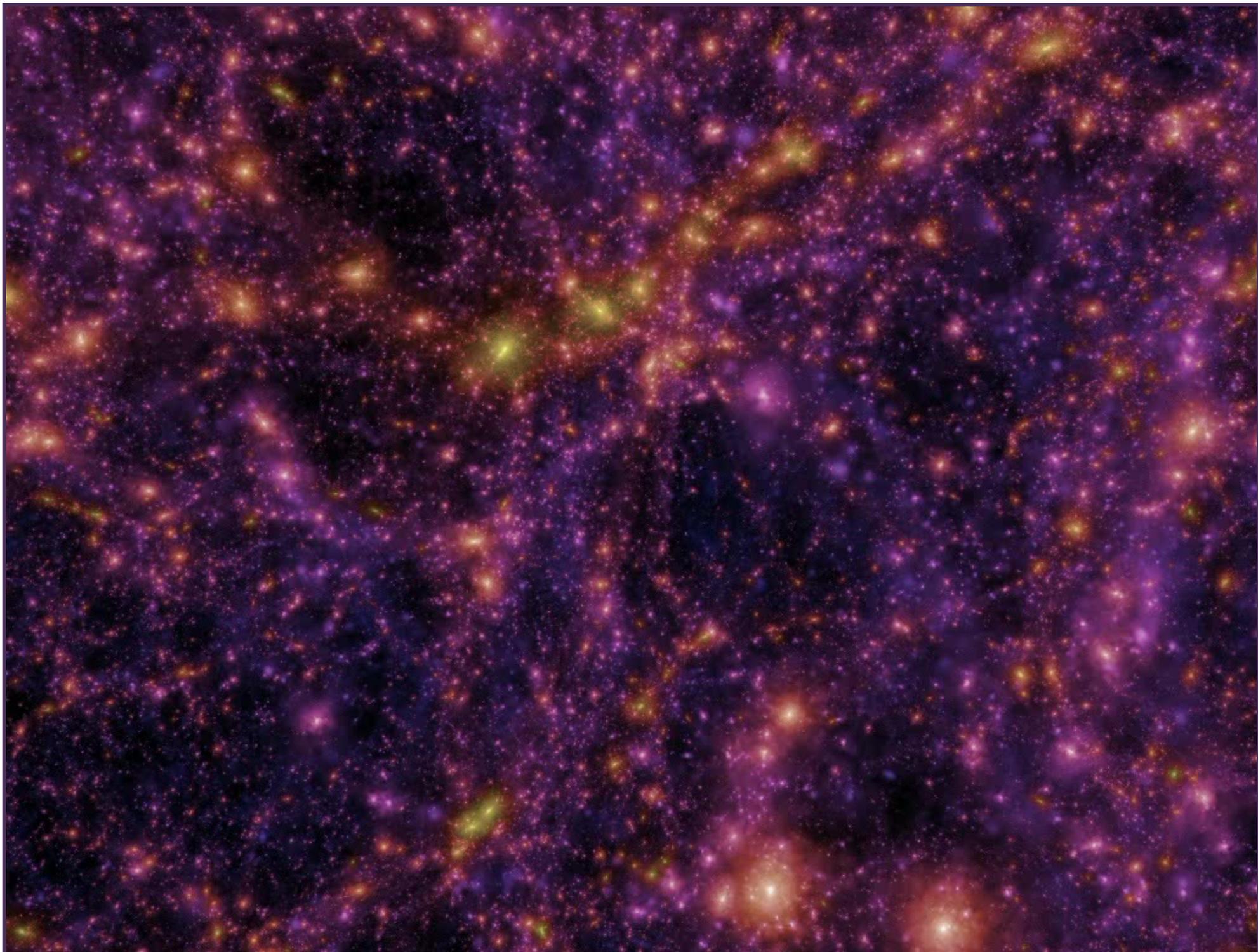
# The 2dF Galaxy Redshift Survey

221,000 redshifts

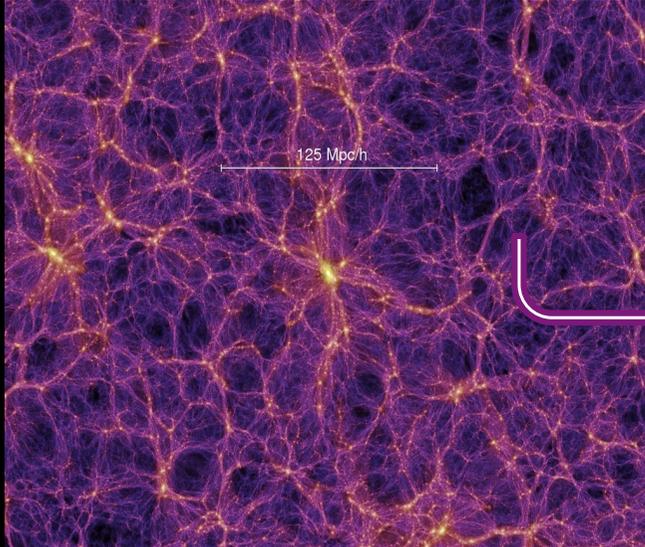
$z \sim 0$



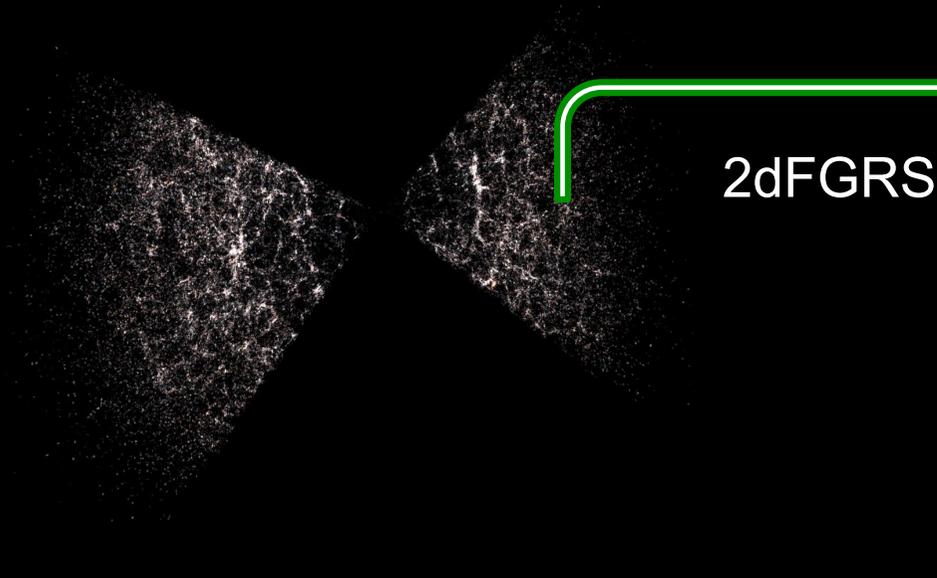
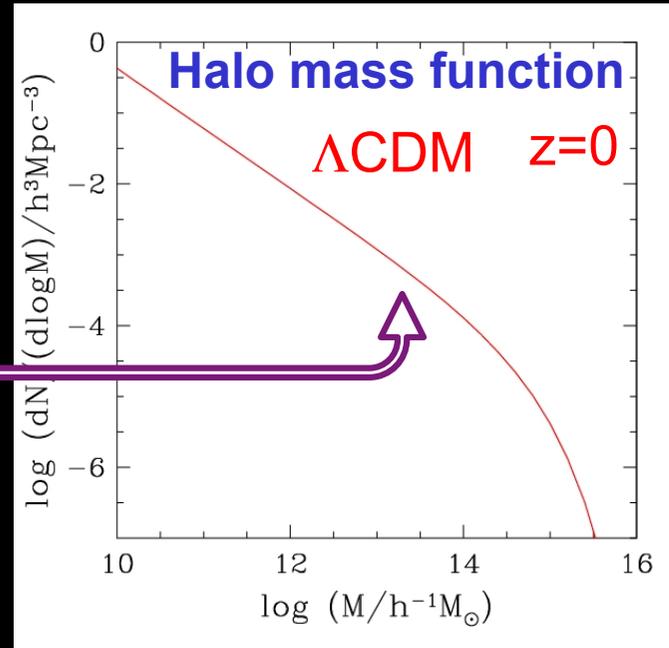
2005



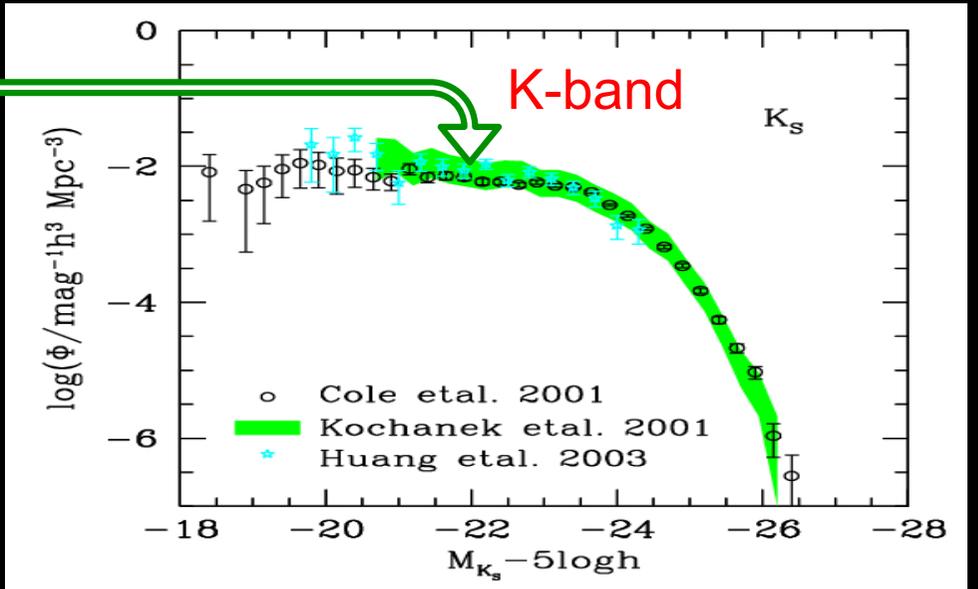
# Abundance of gals & dark halos



Millennium run

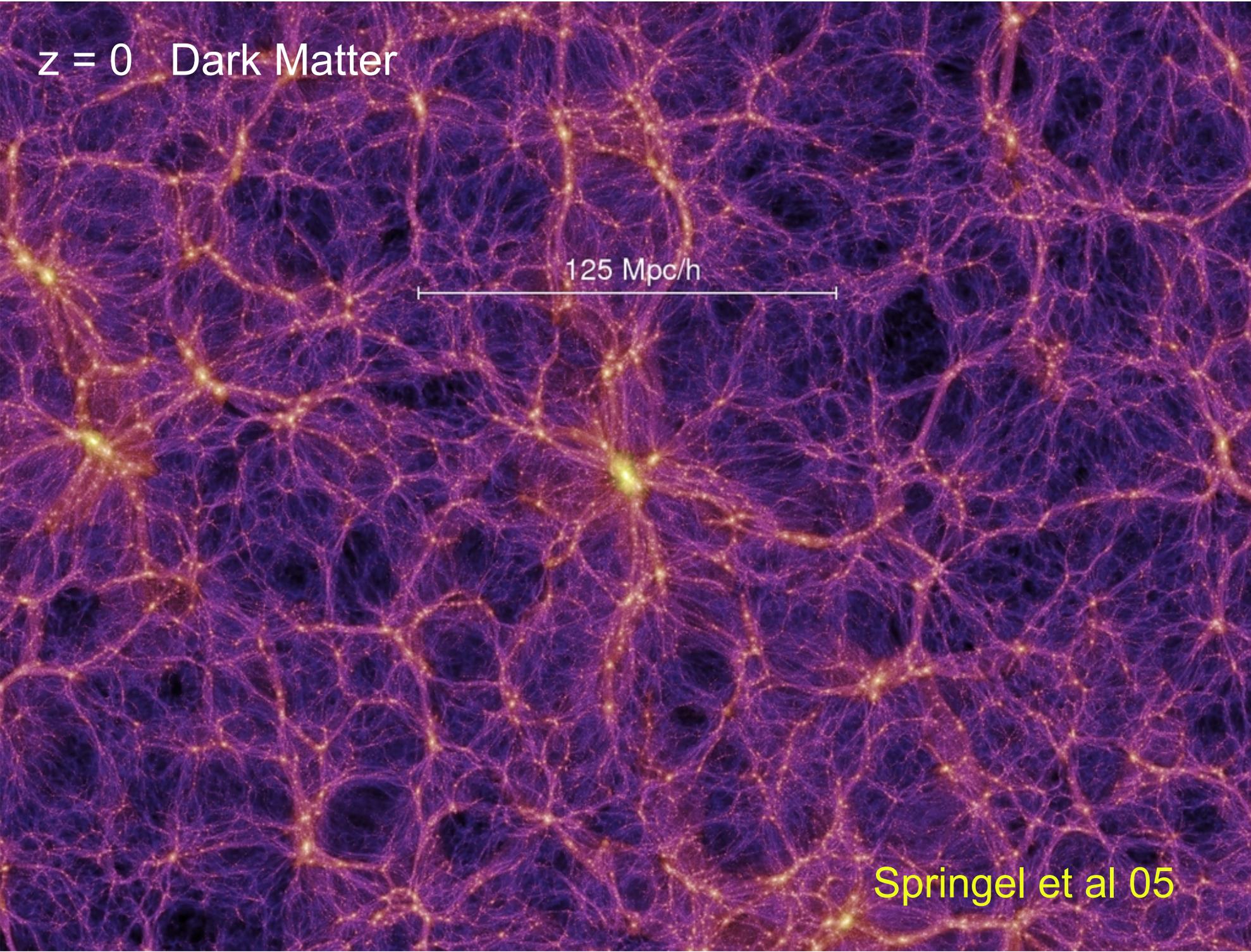


2dFGRS



$z = 0$  Dark Matter

125 Mpc/h



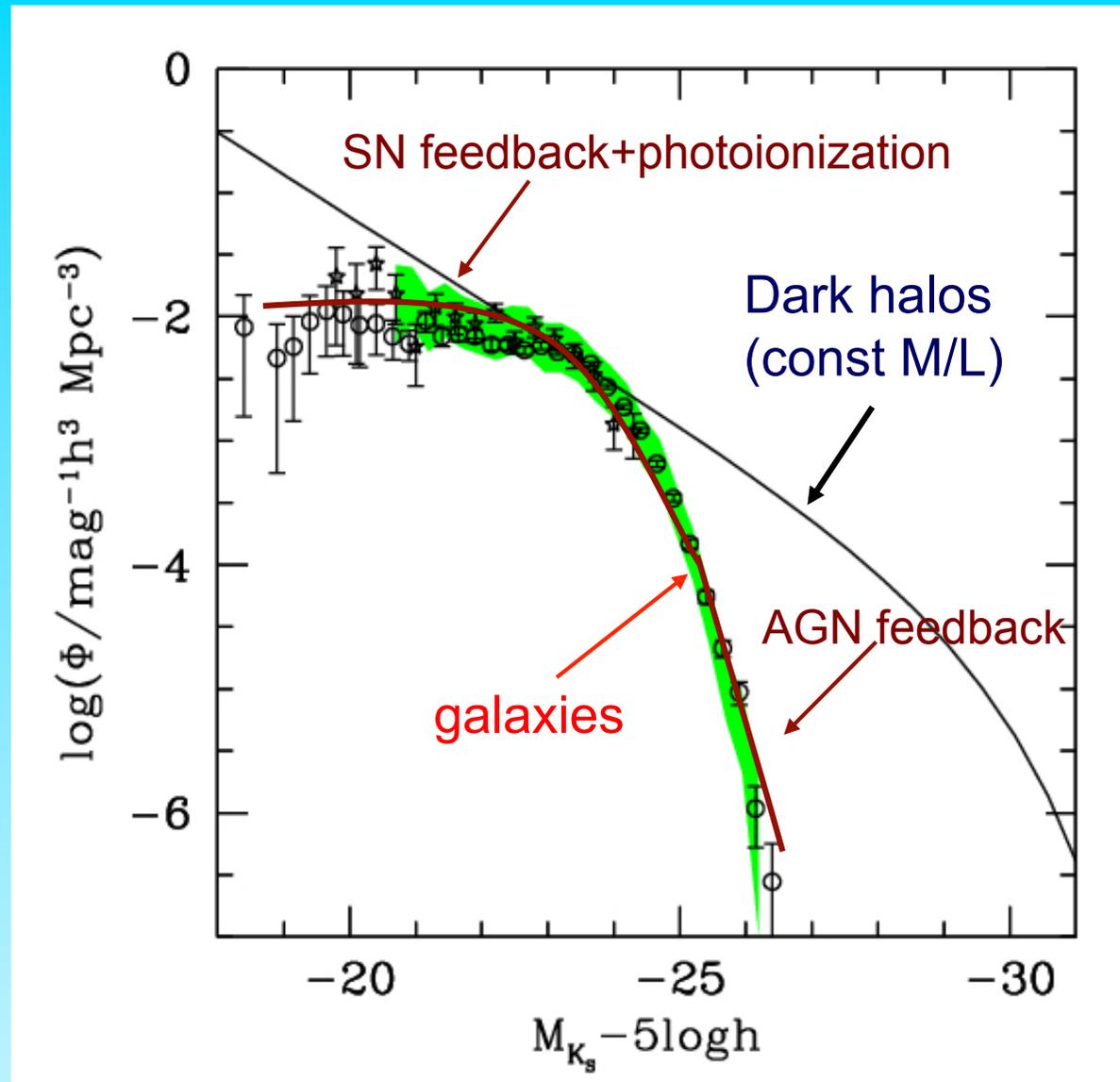
Springel et al 05

# The galaxy luminosity function

The halo mass function and the galaxy luminosity function have different shapes



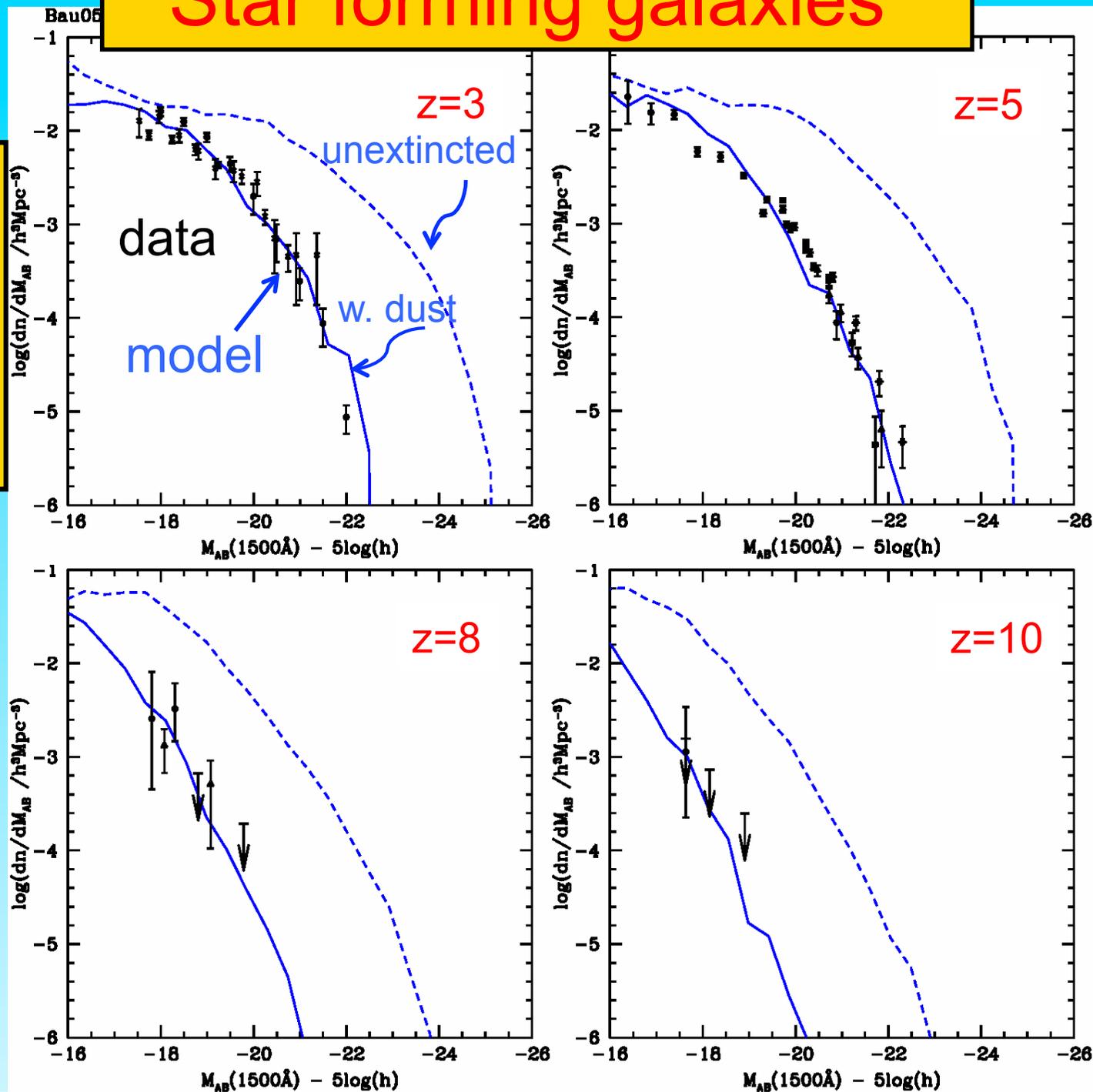
Complicated variation of M/L with halo mass



White & Frenk '91; Kauffmann et al '93; Benson et al '03; Croton et al '05; Bower et al. '06

# Star forming galaxies

## Evolution of Lyman-break galaxy lum. function



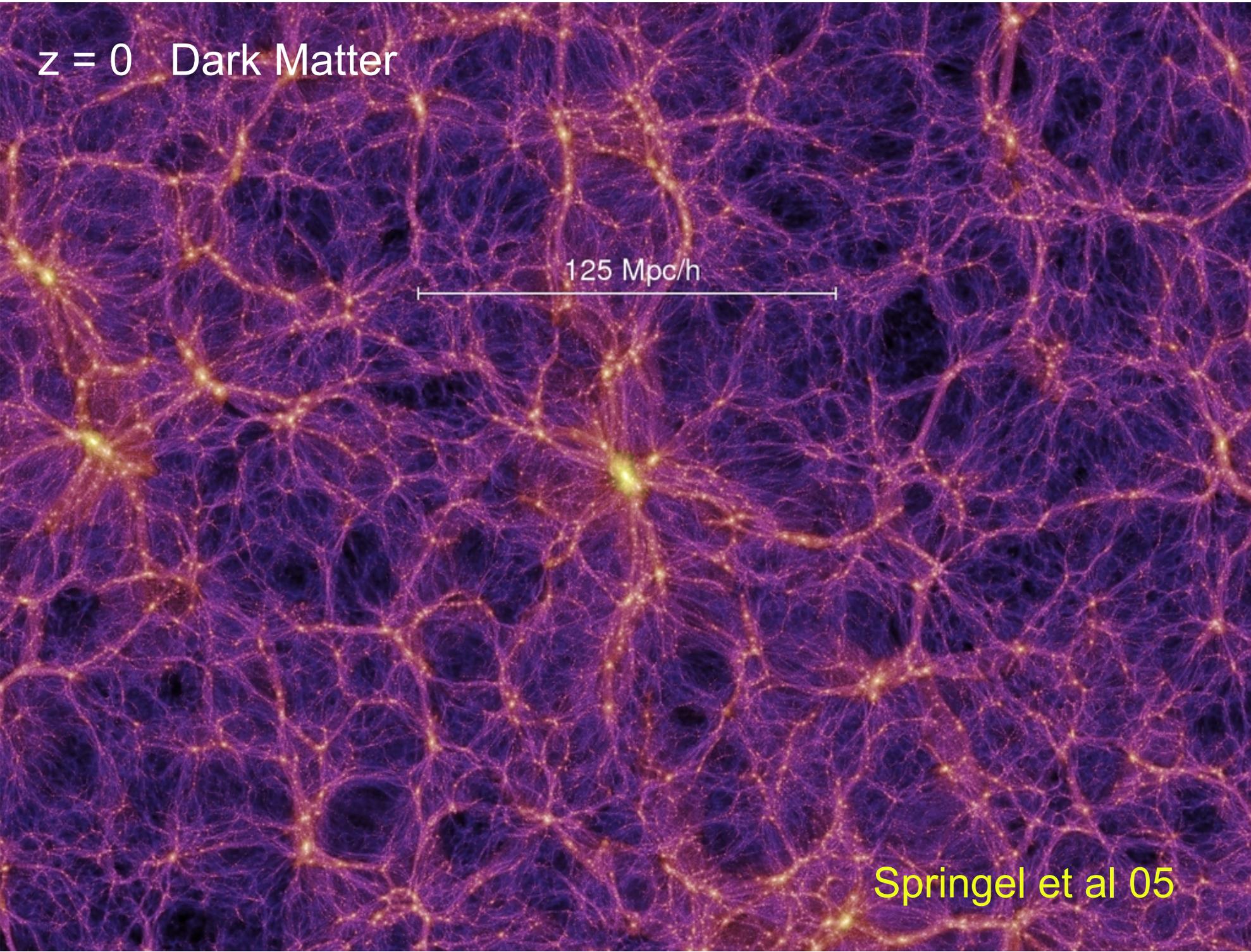
Lacey, Baugh,  
Frenk, Benson '11

Main successes of the CDM cosmogony:

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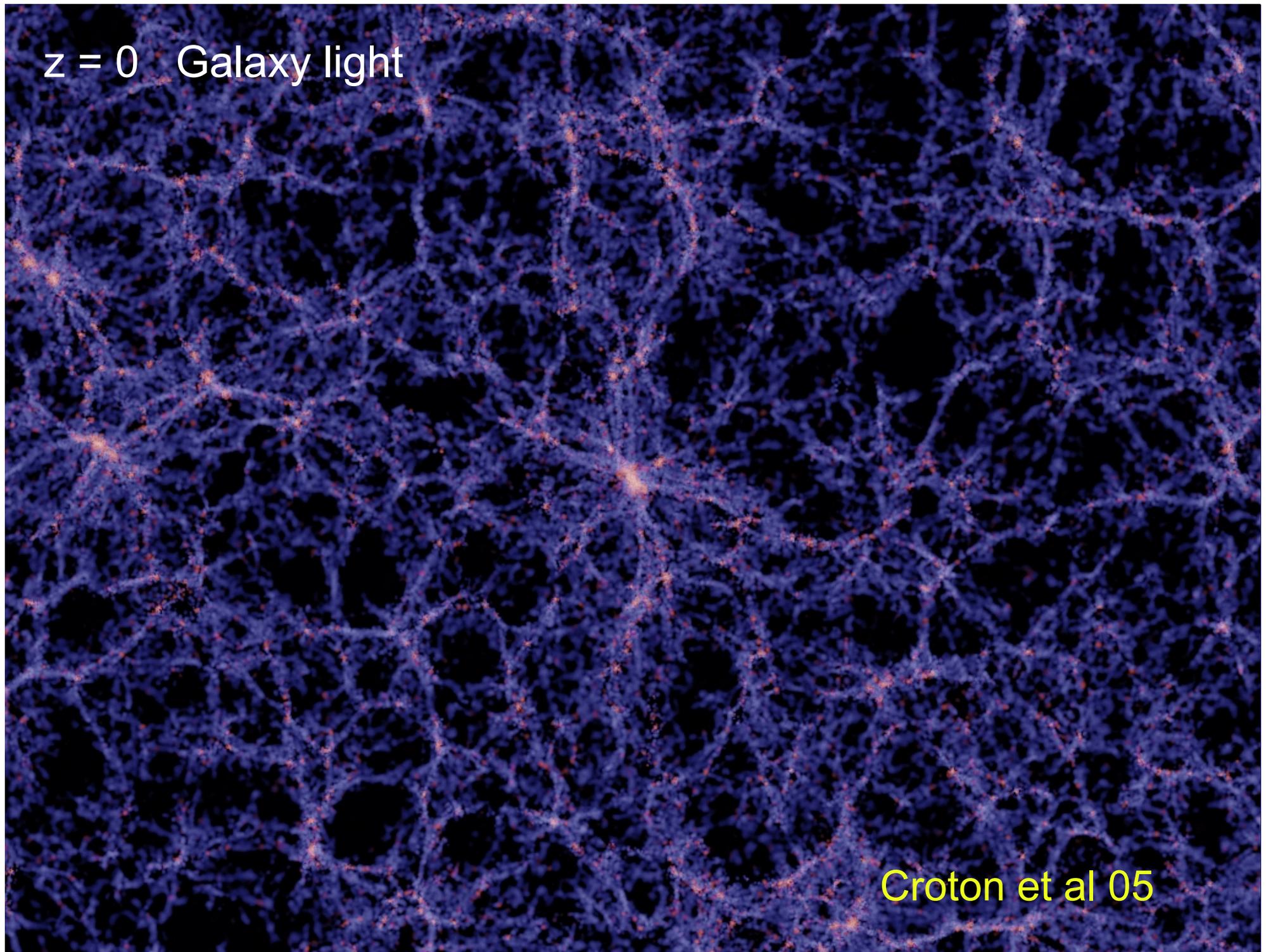
$z = 0$  Dark Matter

125 Mpc/h



Springel et al 05

$z = 0$  Galaxy light

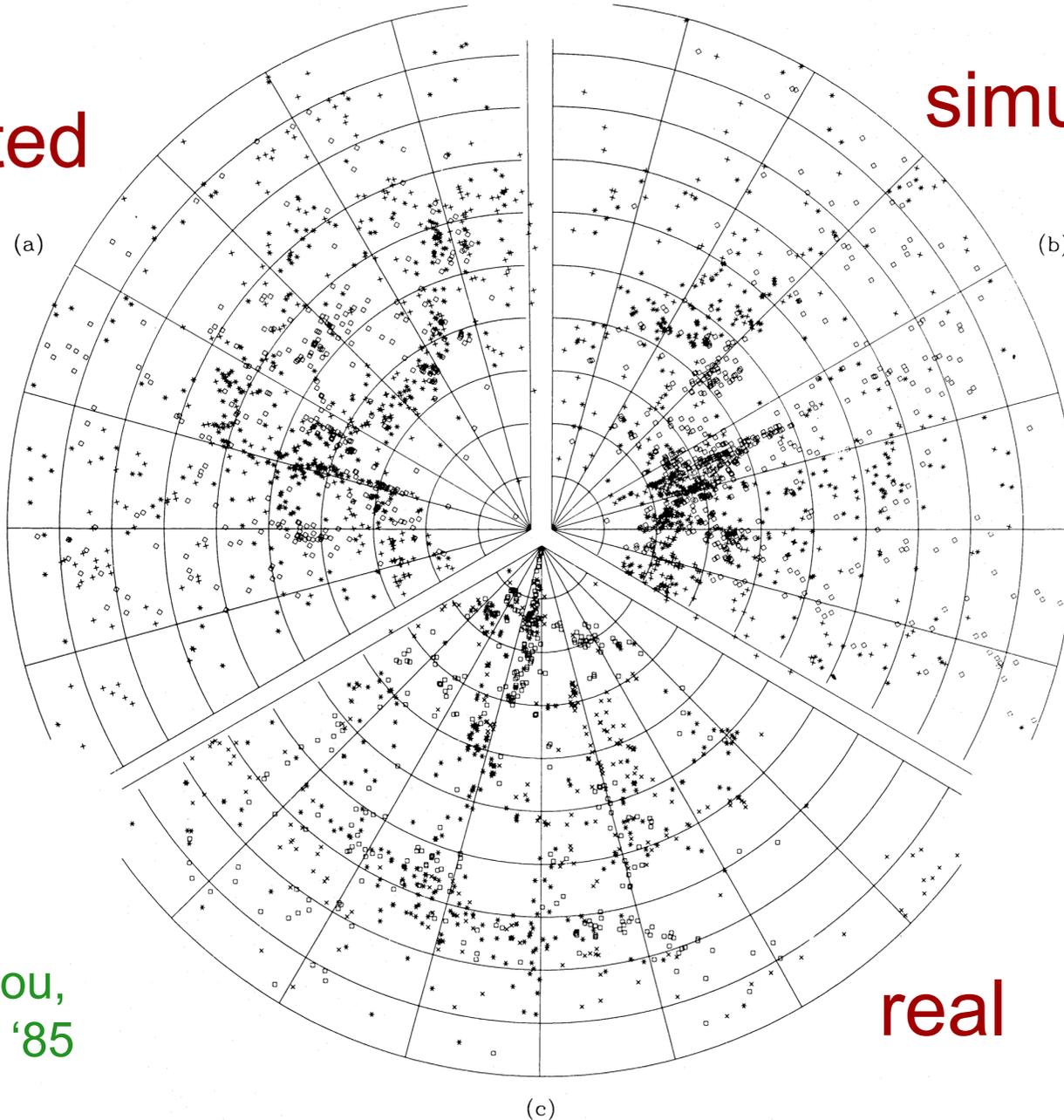


Croton et al 05

# Early simulations of $\Lambda$ CDM

simulated

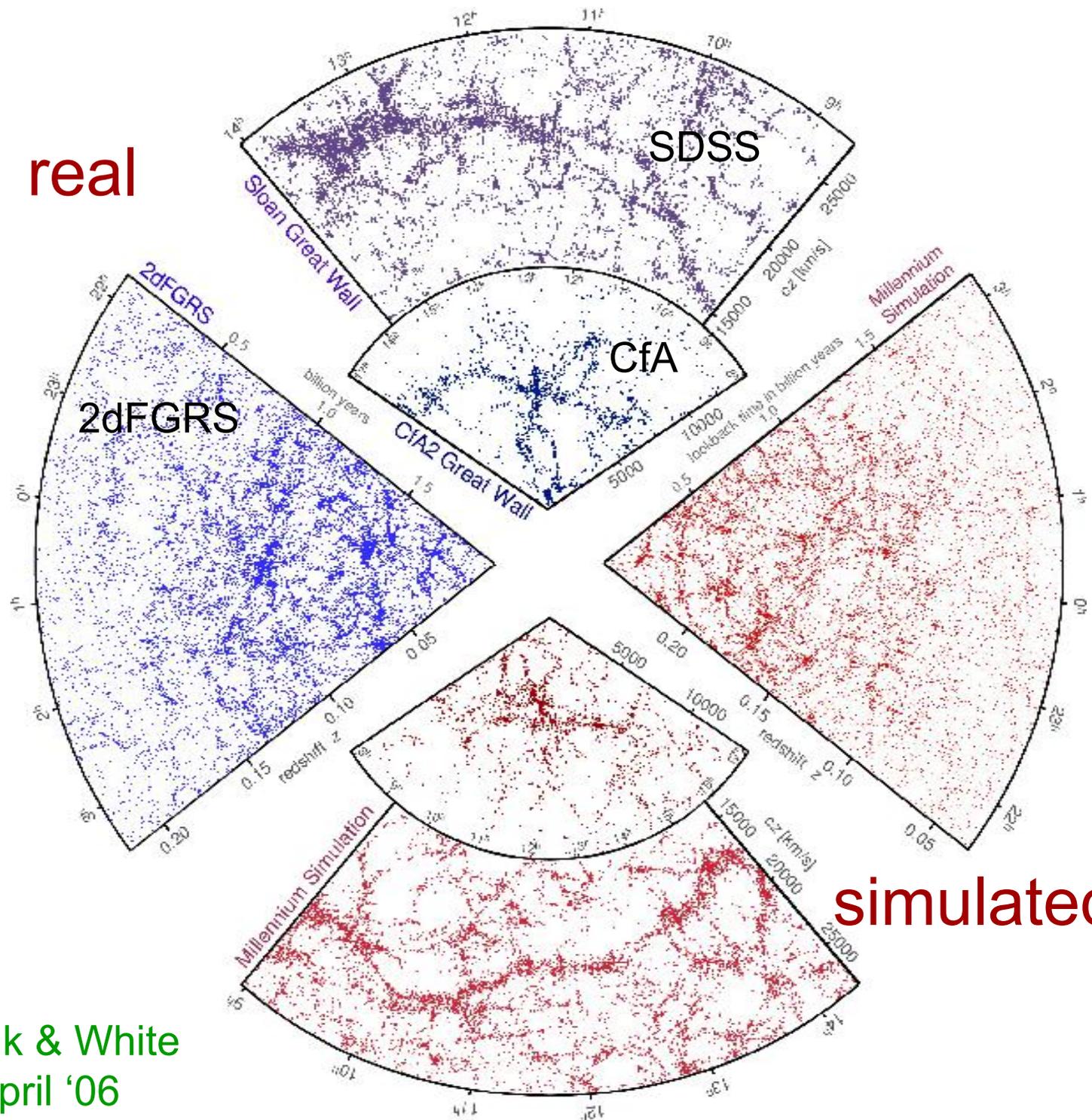
simulated



Davis, Efstathiou,  
Frenk & White '85

real

real

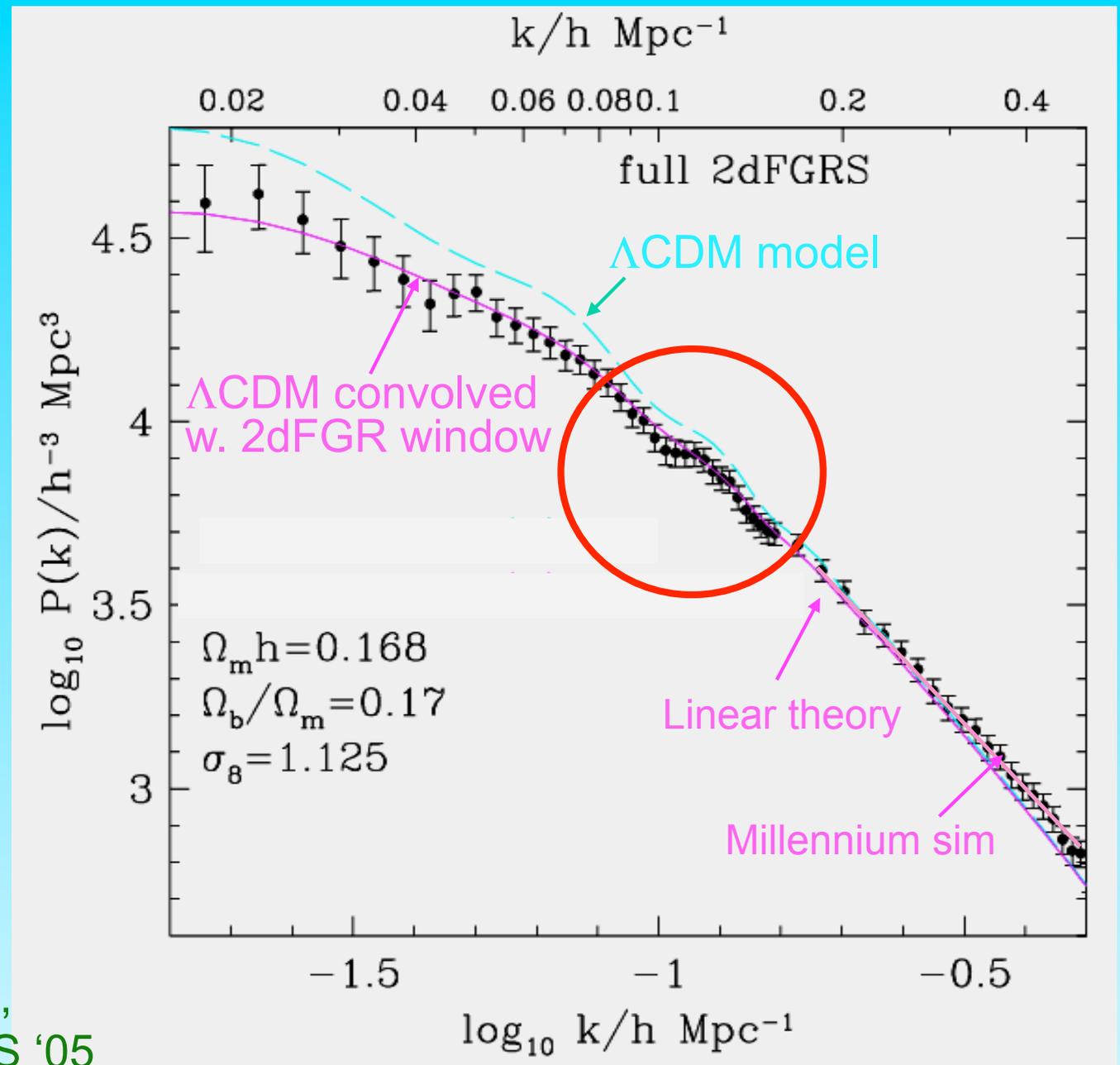


simulated

Springel, Frenk & White  
Nature, April '06

# The final 2dFGRS power spectrum

2dFGRS  $P(k)$   
well fit by  $\Lambda$ CDM  
model convolved  
with window  
function



Cole, Percival, Peacock,  
Baugh, Frenk + 2dFGRS '05

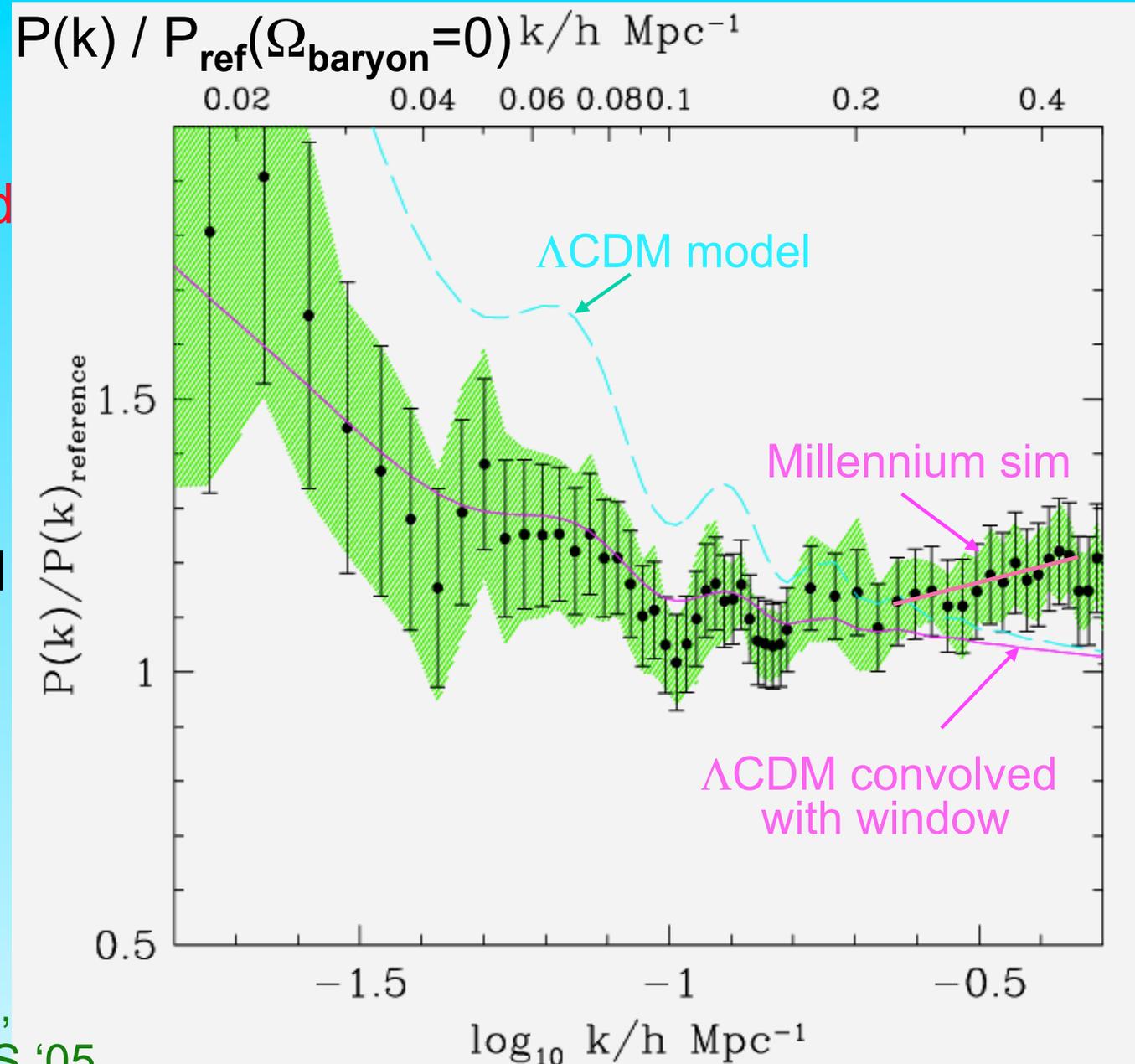
# The final 2dFGRS power spectrum

Baryon oscillations conclusively detected in 2dFGRS!!!

Consistent with structure growth by gravitational instability in a  $\Lambda$ CDM universe

Also detected in SDSS LRG sample (Eisenstein et al 05)

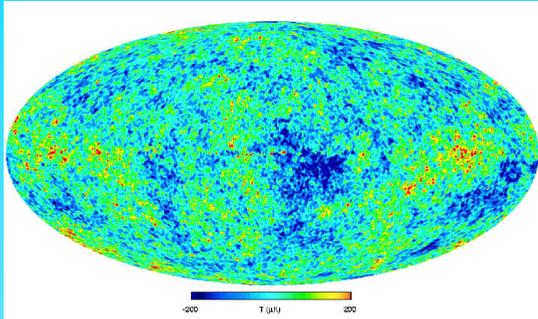
Cole, Percival, Peacock, Baugh, Frenk + 2dFGRS '05



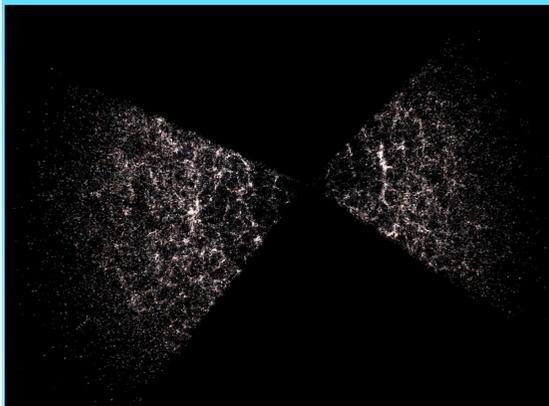
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# The cosmic power spectrum: from the CMB to the 2dFGRS



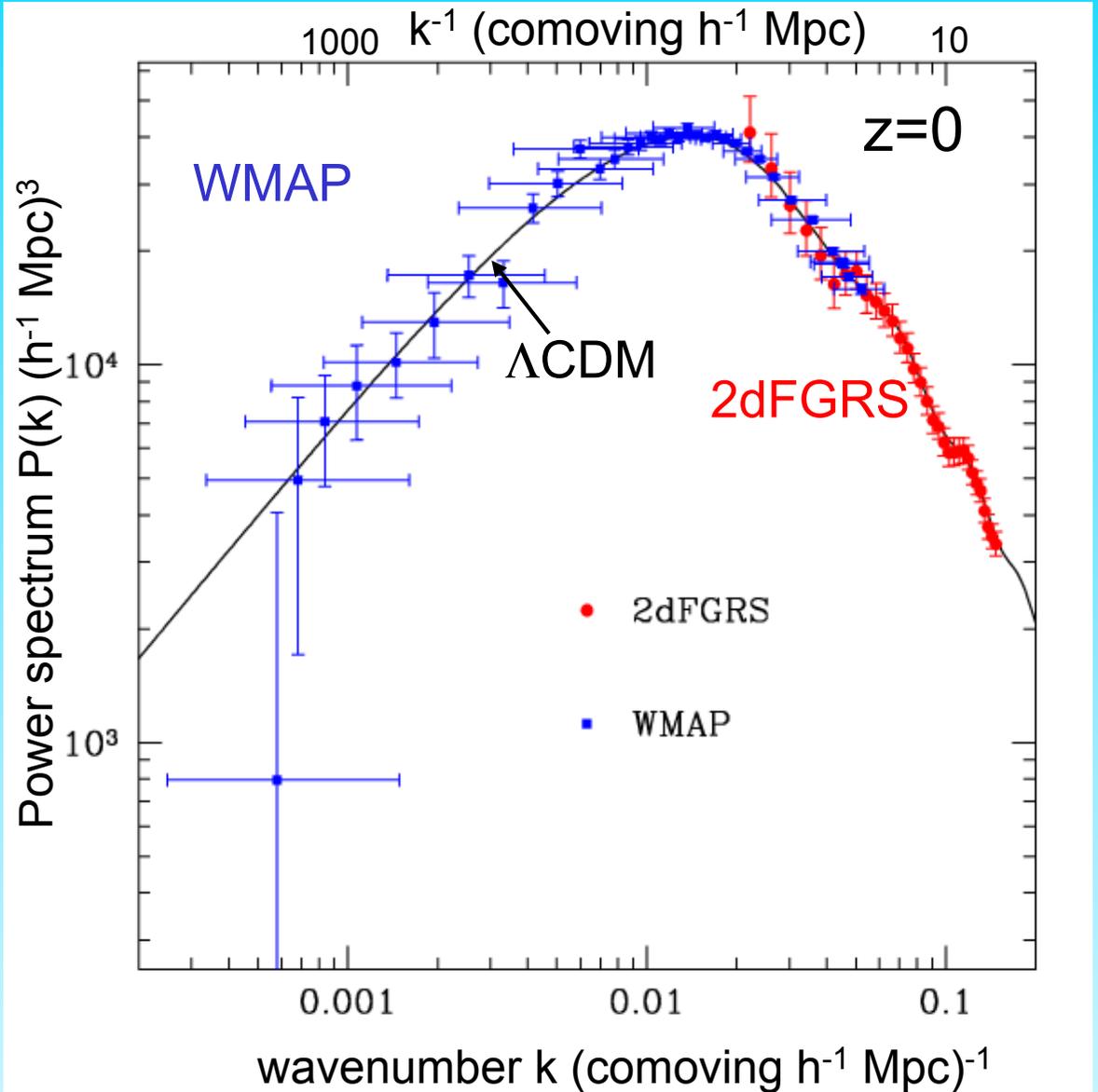
$z \sim 1000$



$z \sim 0$

$\Rightarrow \Lambda\text{CDM}$  provides an excellent description of mass power spectrum from 10-1000 Mpc

Sanchez et al 06



# The dark matter power spectrum

$k^3 P(k)$

The linear power spectrum (“power per octave”)

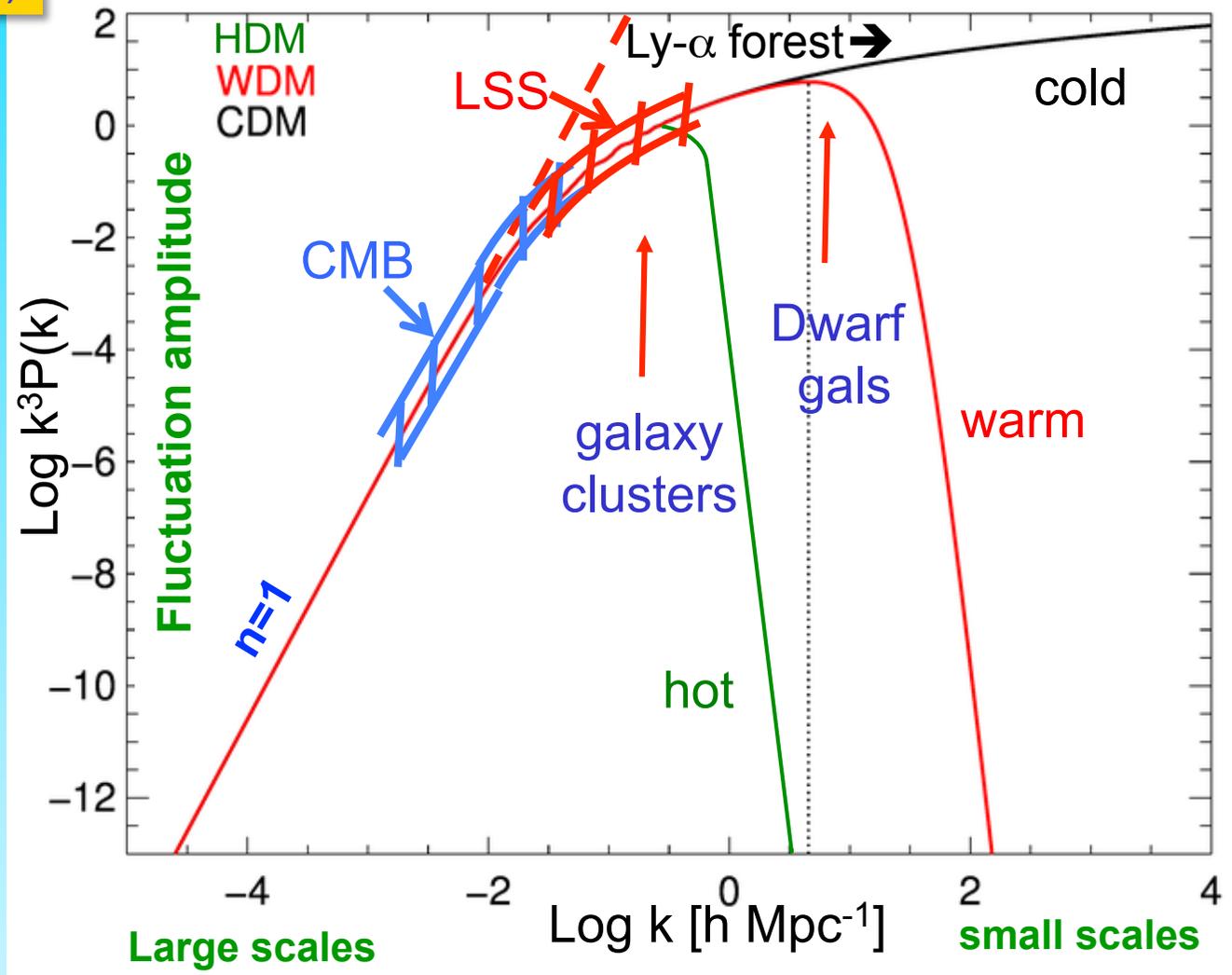
Free streaming →

$\lambda_{\text{cut}} \propto m_x^{-1}$   
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$m_{\text{CDM}} \sim 100\text{GeV}$   
susy;  $M_{\text{cut}} \sim 10^{-6} M_{\odot}$

$m_{\text{WDM}} \sim \text{few keV}$   
sterile  $\nu$ ;  $M_{\text{cut}} \sim 10^9 M_{\odot}$

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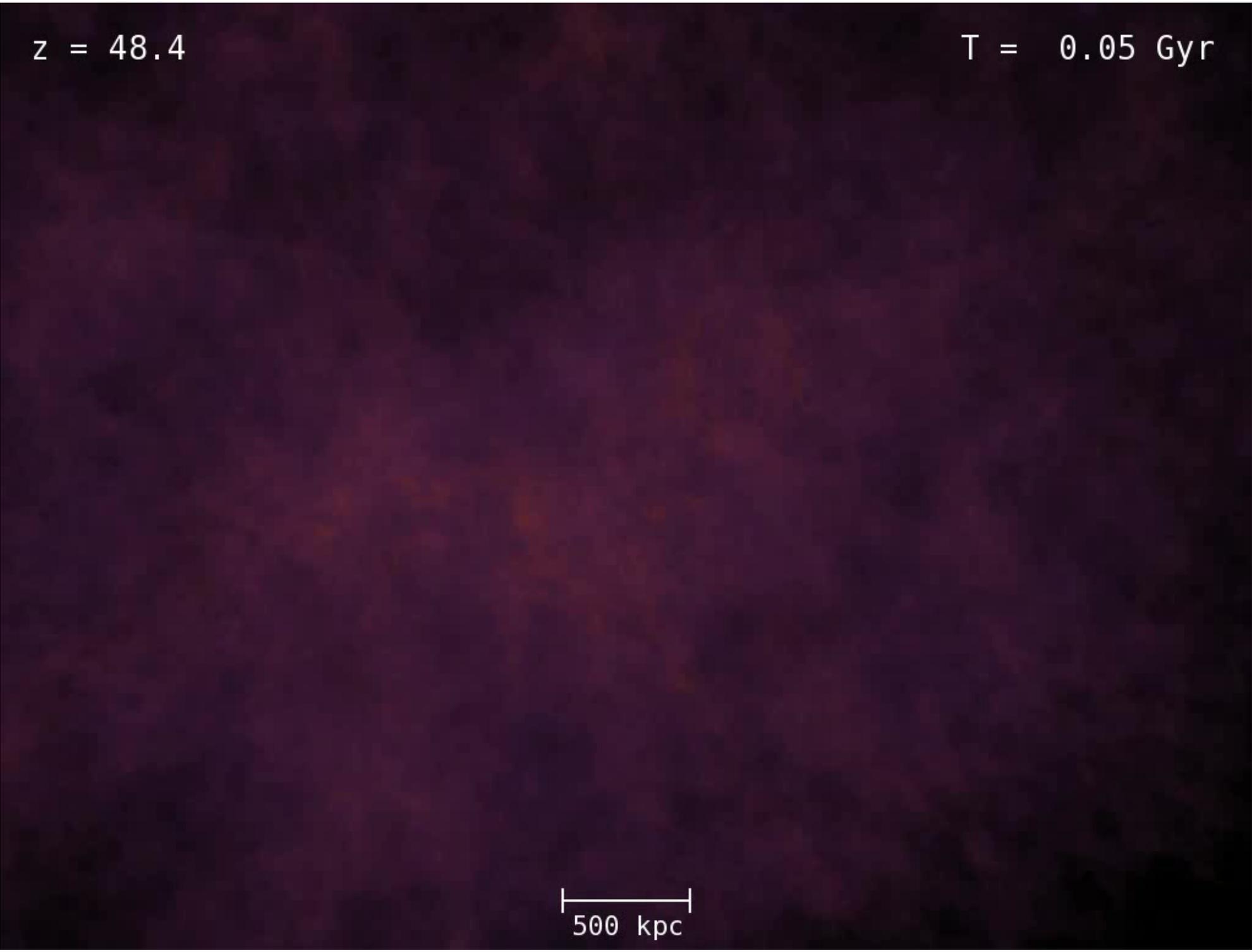
Cosmology on small – **strongly  
non-linear** – scales

→ key to the identity of the dark matter

$z = 48.4$

$T = 0.05 \text{ Gyr}$

500 kpc

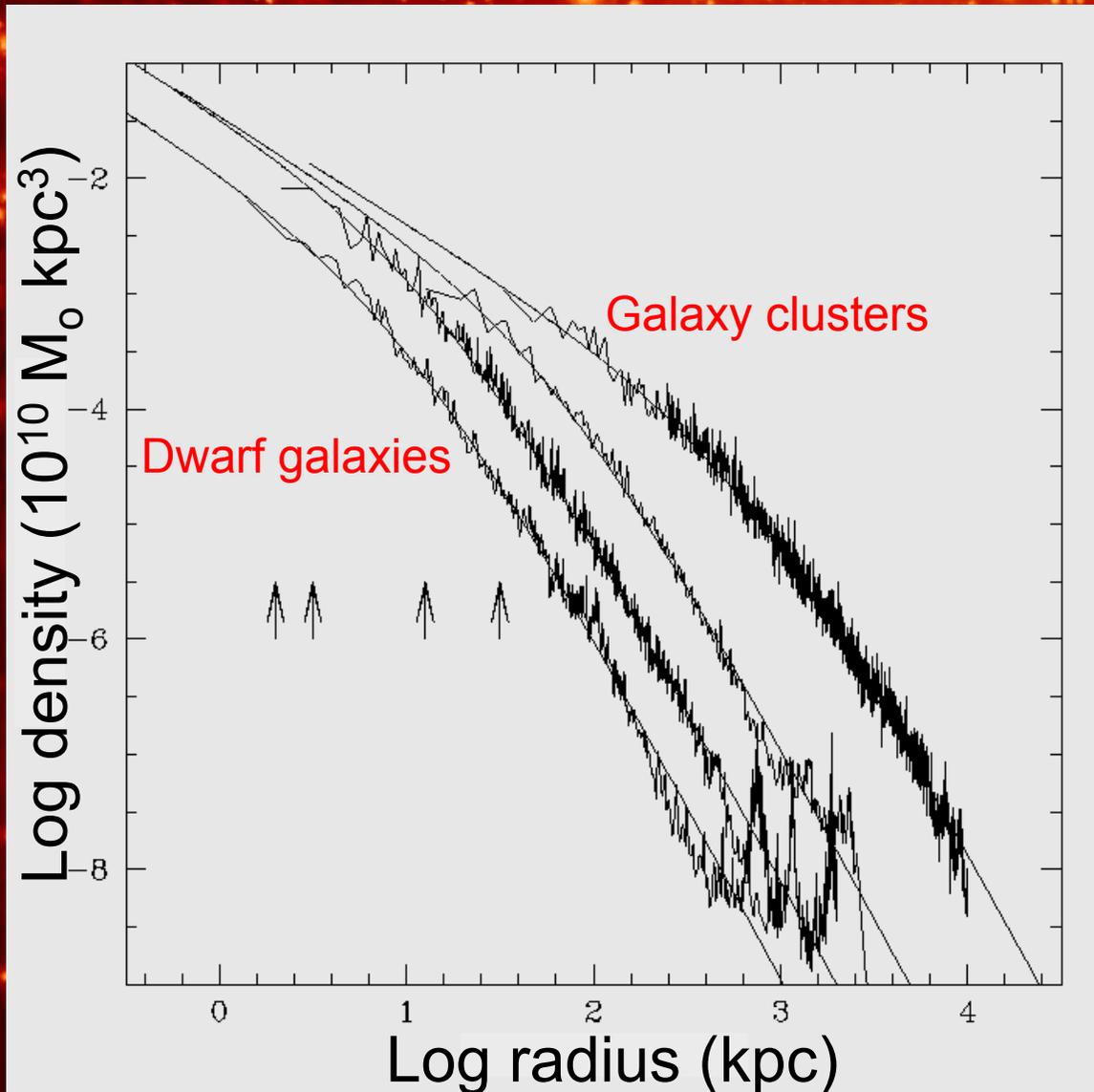


# A cold dark matter universe

CDM N-body simulations make two important predictions on non-linear (halo) scales:

- The main halo and its subhalos have “cuspy” density profiles
- Large number of self-bound substructures (**10% of mass**) survive

# The Density Profile of Cold Dark Matter Halos



Halo density profiles are independent of halo mass & cosmological parameters

There is no obvious density plateau or 'core' near the centre.

(Navarro, Frenk & White '97)

$$\frac{\rho(r)}{\rho_{crit}} = \frac{\delta_c}{(r/r_s)(1+r/r_s)^2}$$

Halos that form earlier have higher densities (bigger  $\delta$ )

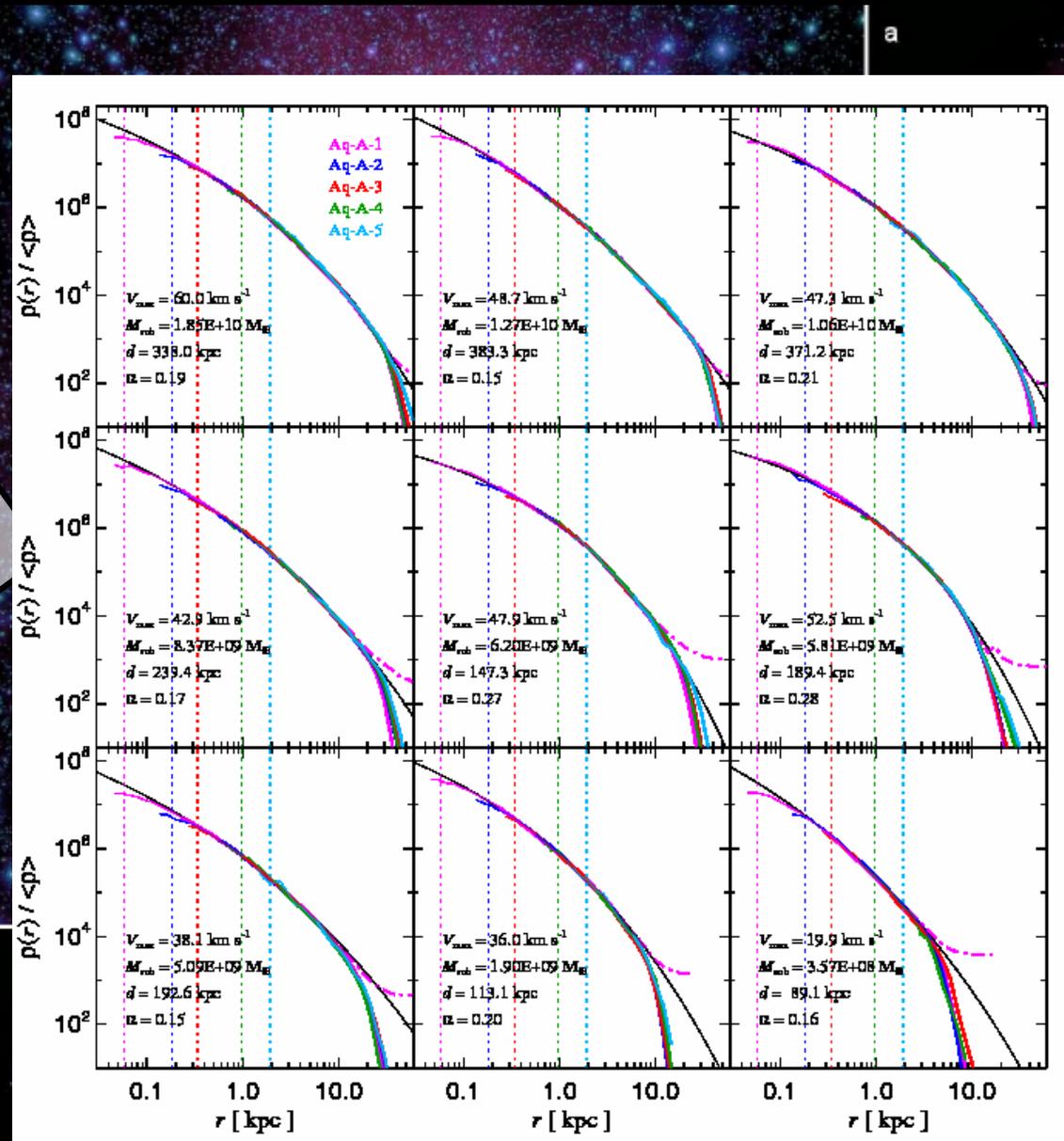


VIRG

CDM subhalos also have cuspy profiles

Aquarius

Springel et al '08





cold dark matter

warm dark matter



Lovell, Eke, Frenk, Gao, Jenkins, Wang, White, Theuns,  
Boyarski & Ruchayskiy '12

# A warm dark matter universe

For viable WDM particle masses, there is little difference between CDM and WDM on scales larger than galaxies.

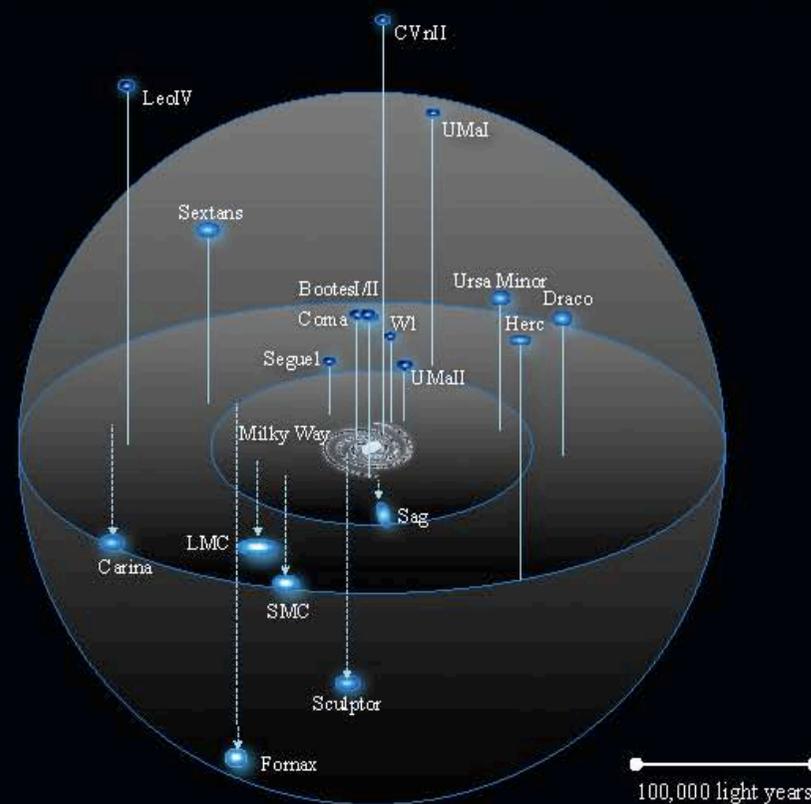
## On subgalactic scales:

- Subhalos still “cuspy” but less concentrated than in CDM
- Far fewer self-bound substructures (**3% of mass**) survive

→ Can test for identity of the dark matter!

# The satellites of the Milky Way

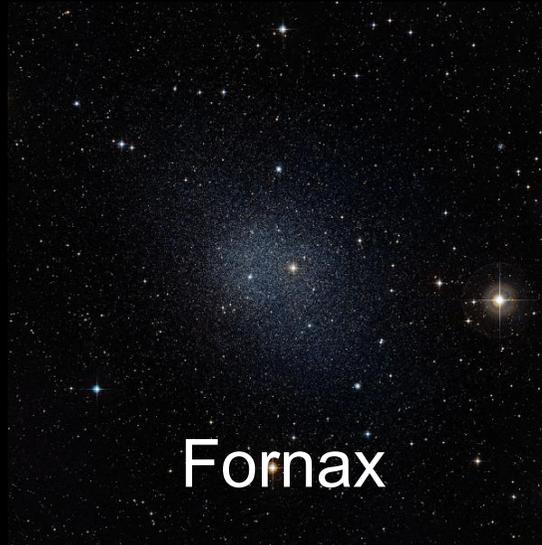
~25 satellites known  
in the MW



J. Bullock



# Dwarf galaxies around the Milky Way



## Dwarf sphs: cores or cusps?

Jeans eqn:

$$\frac{GM(r)}{r} = -\sigma_r^2 \left[ \frac{d \ln \rho_*}{d \ln r} + \frac{d \ln \sigma_r^2}{d \ln r} + 2\beta \right]$$

stellar density profile radial velocity dispersion  
↙ ↘  
↑ ↑  
from Aquarius sim vel. anisotropy

## Dwarf sphs: cores or cusps?

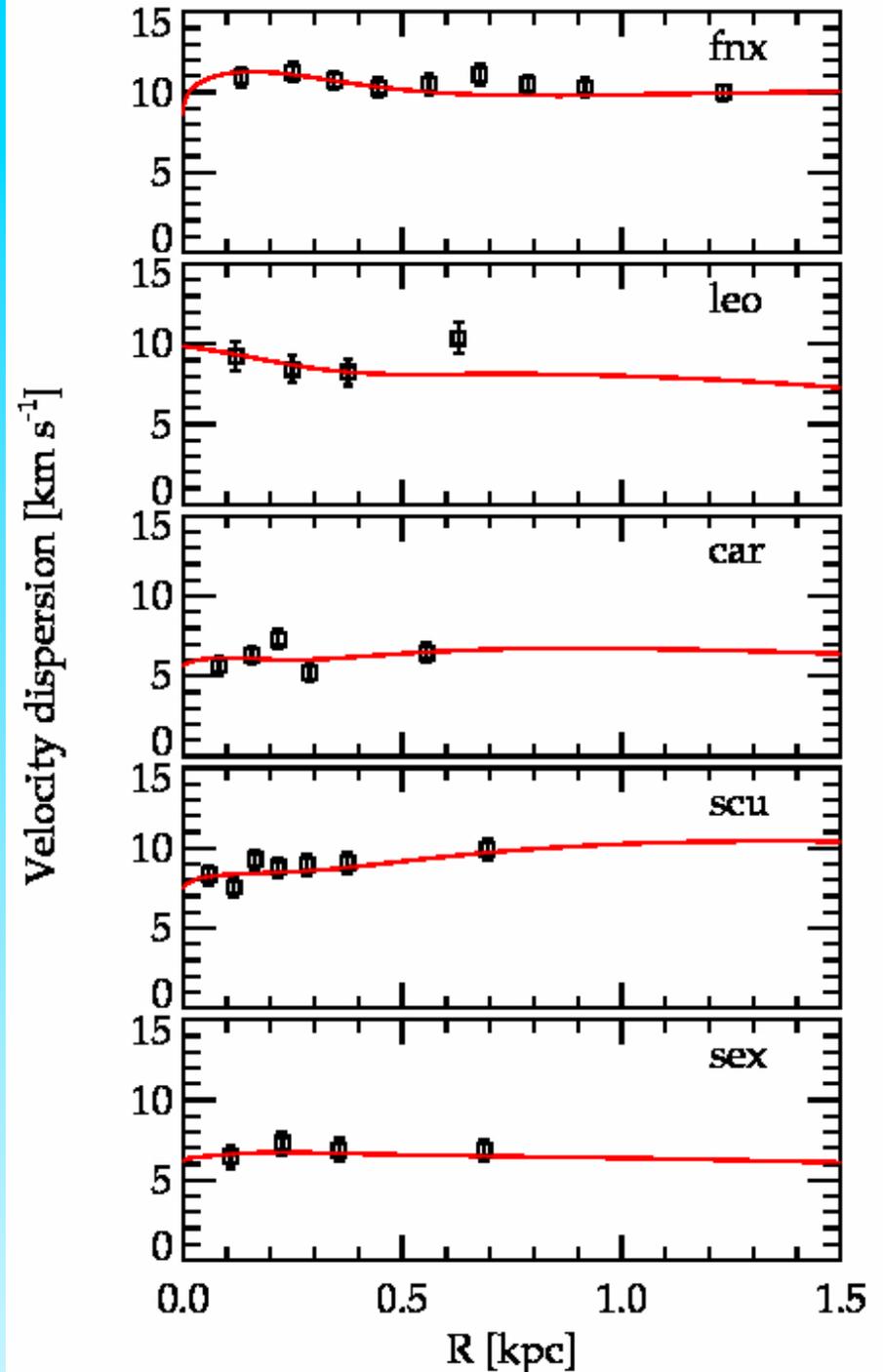
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↑
↑  
 from Aquarius sim                      vel. anisotropy

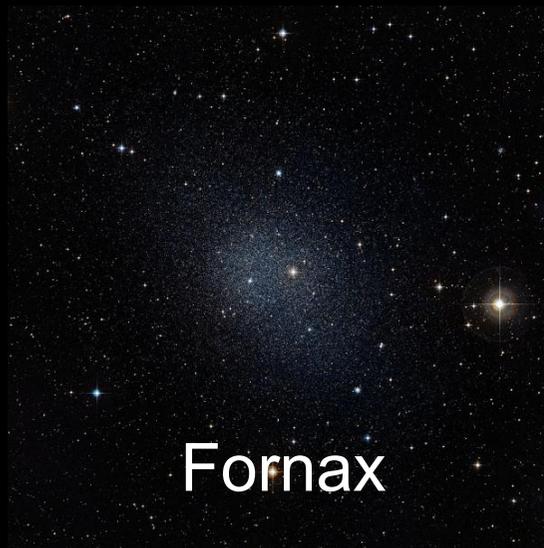
- Assume isotropic orbits
- Solve for  $\sigma_r(r)$
- Compare with observed  $\sigma_r(r)$
- Find “best fit” subhalo

Strigari, Frenk & White 2010





# Dwarf galaxies around the Milky Way



Fornax



Sculptor



Leo I



Sextans



Carina



Sagittarius

Cuspy NFW profiles consistent with MW satellite kinematic data



Halo structure of dwarf satellites  
seems **OK** in **both**  $\Lambda$ CDM and WDM

How can we distinguish between CDM & WDM ?



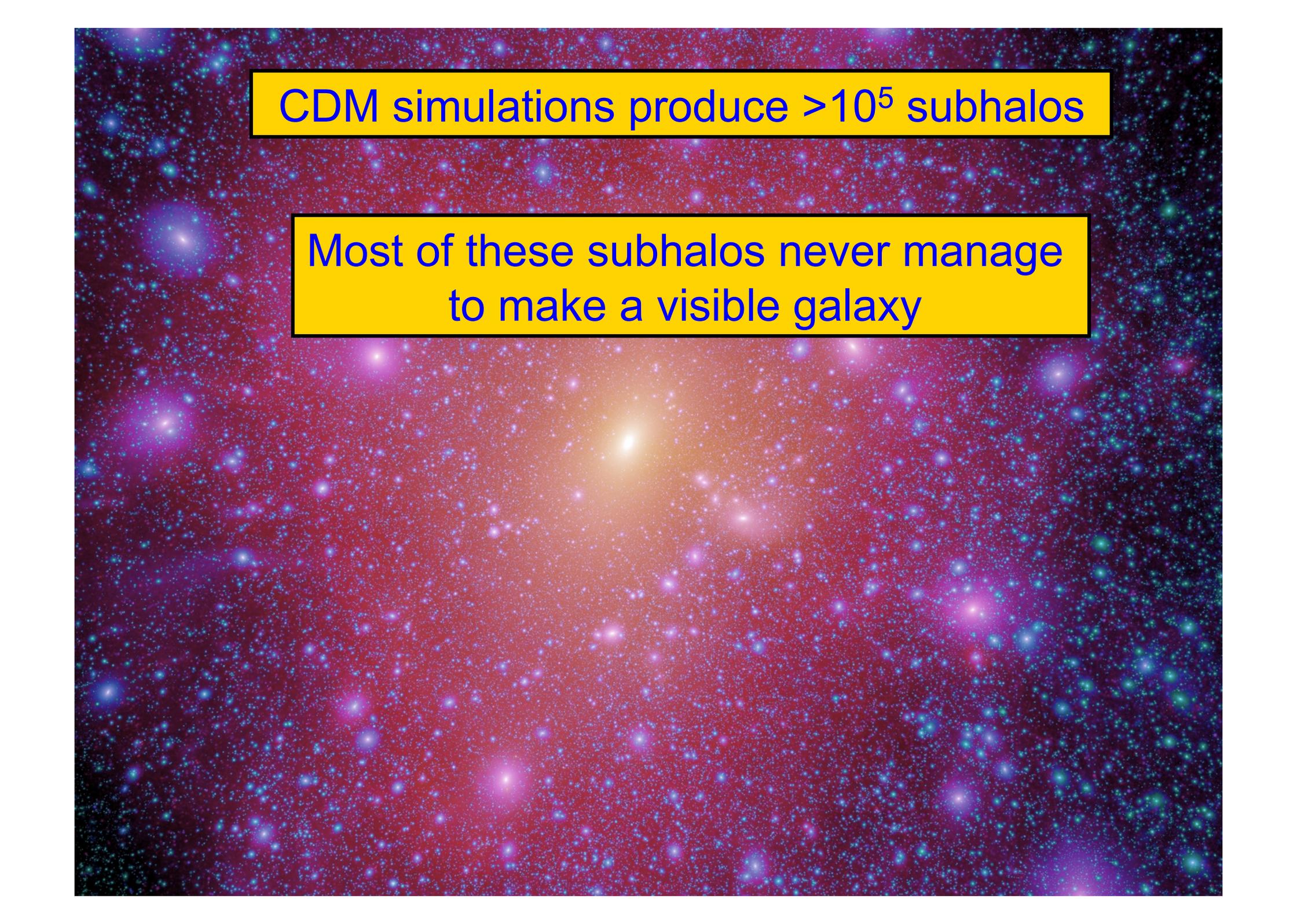
cold dark matter

warm dark matter



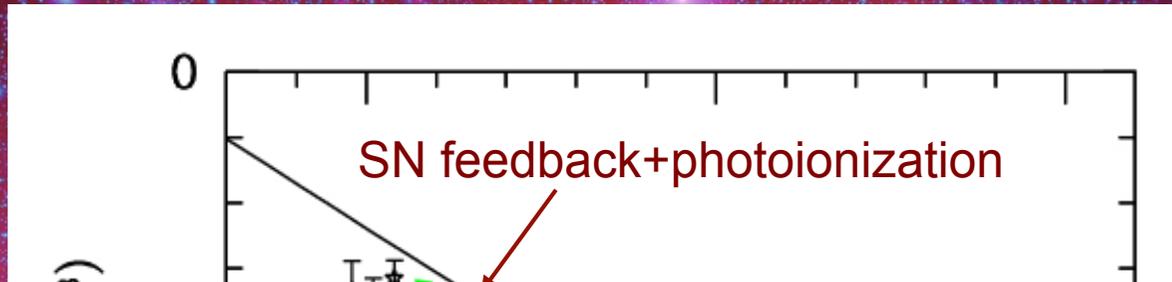
Lovell, Eke, Frenk, Gao, Jenkins, Wang, White, Theuns,  
Boyarski & Ruchayskiy '12

Institute for Computational Cosmology



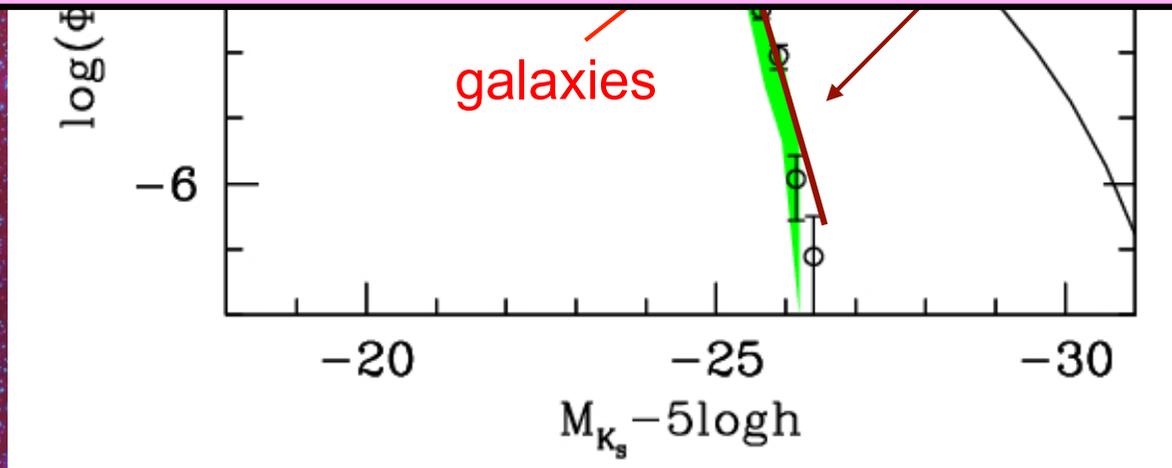
CDM simulations produce  $>10^5$  subhalos

Most of these subhalos never manage  
to make a visible galaxy



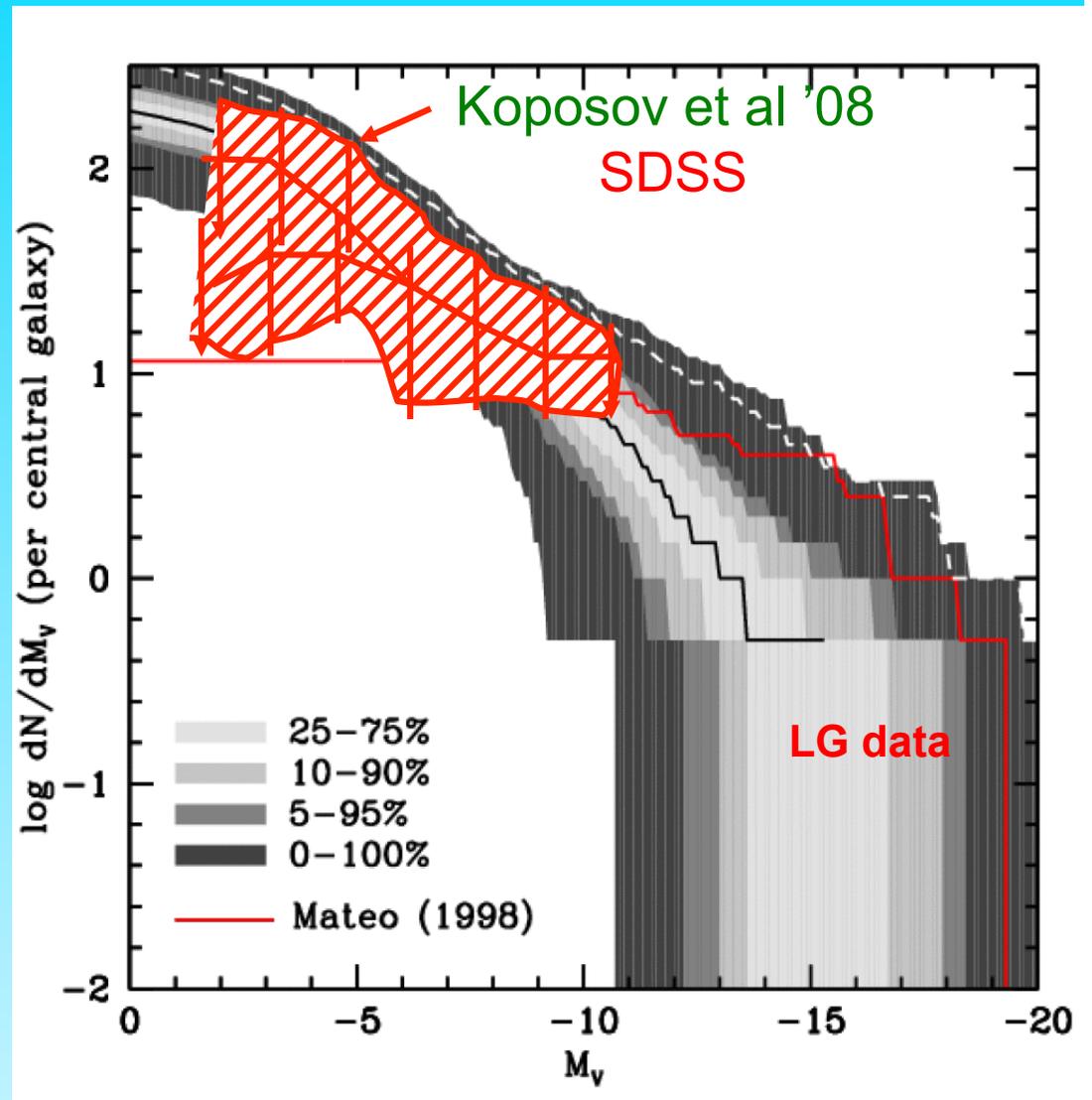
Making a galaxy in a small halo is hard because:

- Early reionization heats gas above  $T_{\text{vir}}$
- Supernovae feedback expels gas



# Luminosity Function of Local Group Satellites

- Median model  $\rightarrow$  correct abund. of sats brighter than  $M_V = -9$  and  $V_{\text{cir}} > 12$  km/s
- Model predicts many, as yet undiscovered, faint satellites
- LMC/SMC should be rare ( $\sim 2\%$  of cases)





cold dark matter

warm dark matter

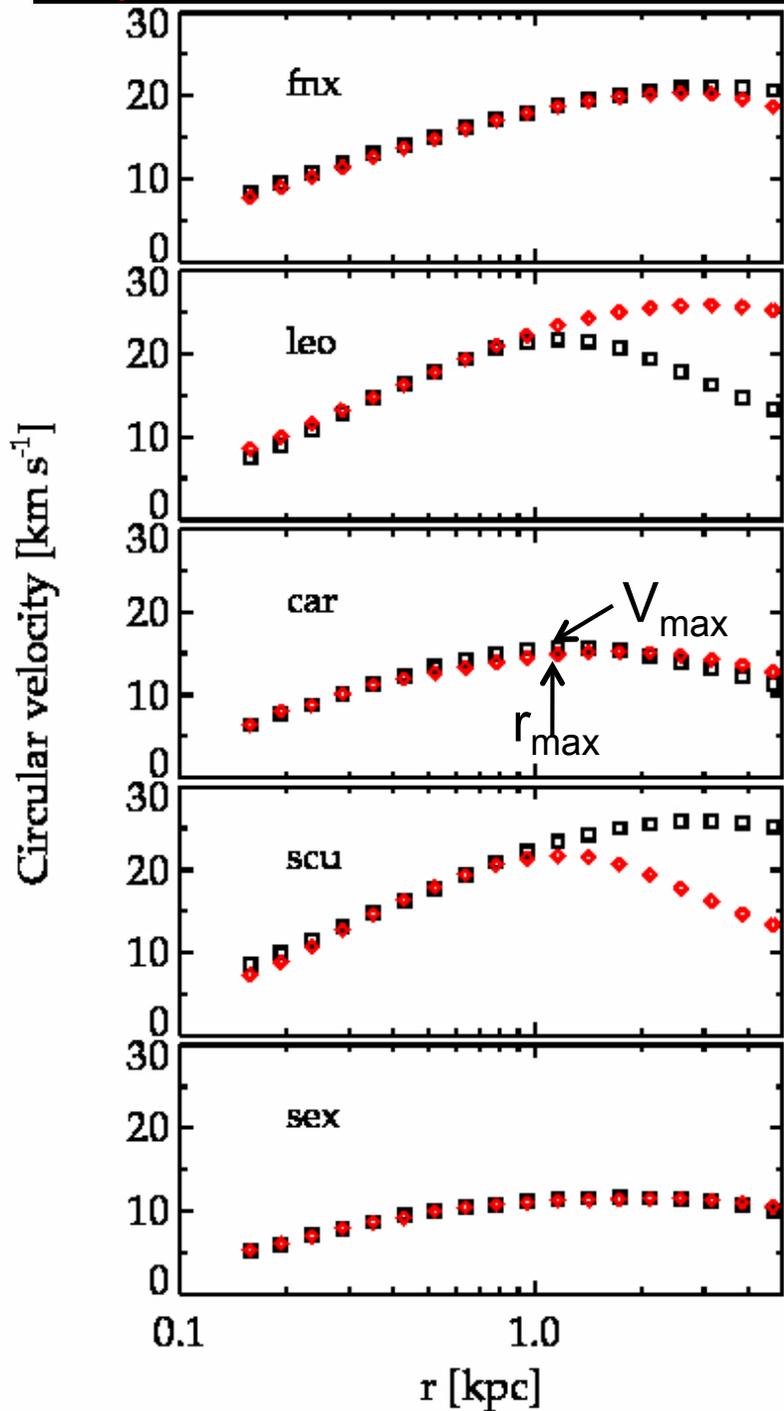
Counting satellites cannot distinguish CDM from WDM!

Need to look in more detail at the structure of small halos

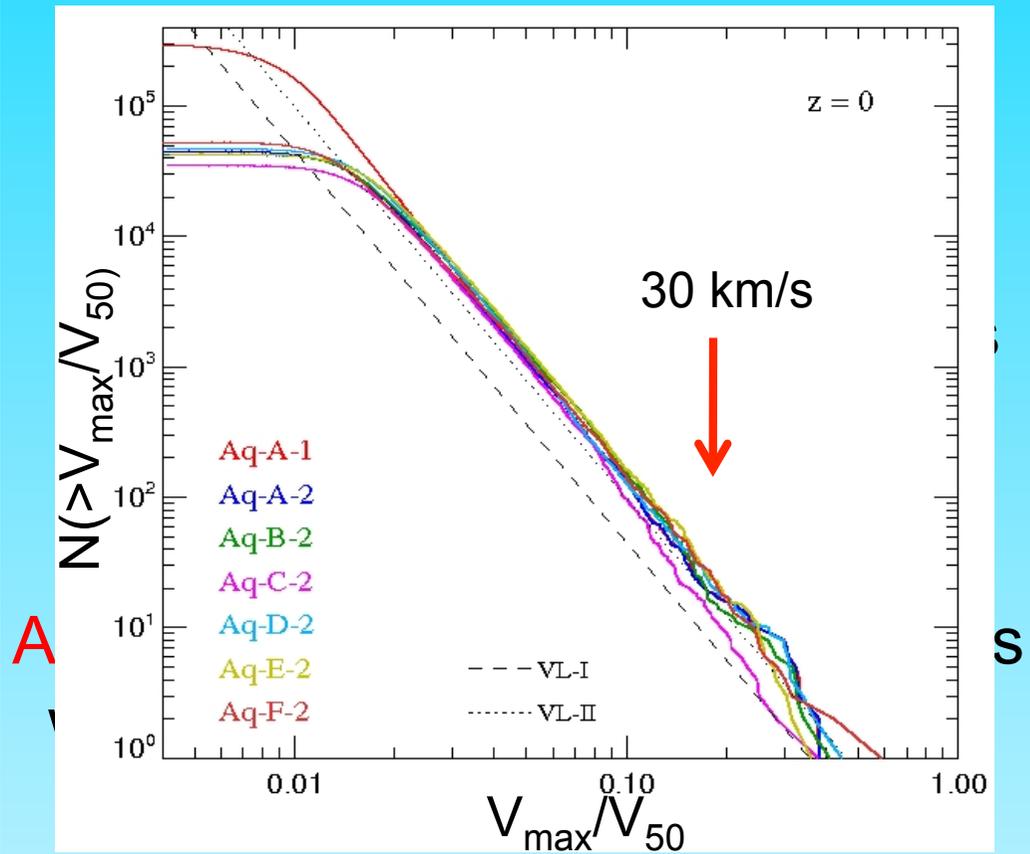
Lovell, Eke, Frenk, Gao, Jenkins, Wang, White, Theuns,  
Boyarski & Ruchayskiy '12

Institute for Computational Cosmology

Top 2 best fit CDM models to data



The Aquarius subhalos and the satellites of the Milky Way



Strigari, Frenk & White 2010

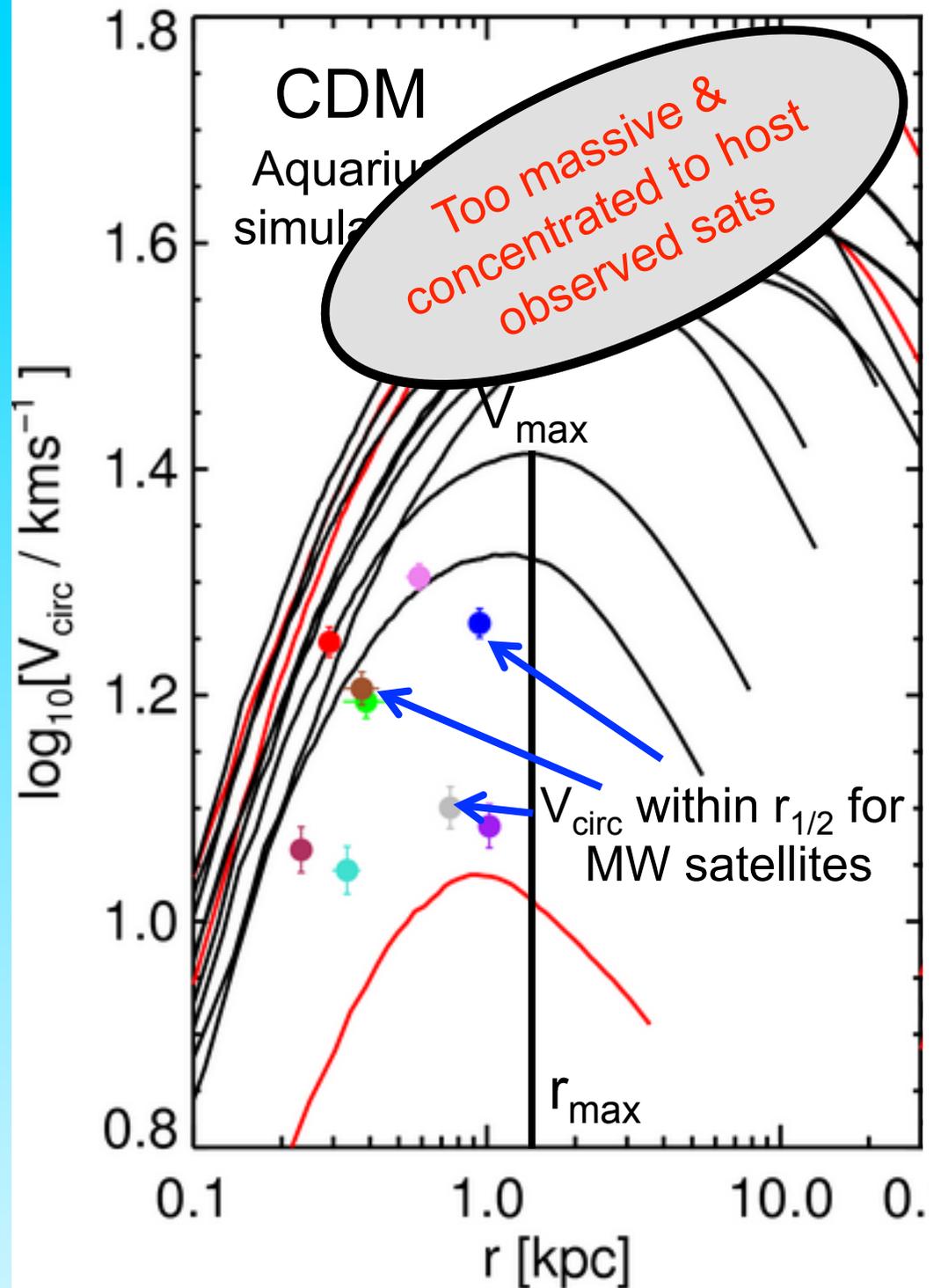
# Is CDM compatible w. luminosity & structure of observed satellites?

$$V_c = \sqrt{\frac{GM}{r}} \quad V_{\max} = \max V_c$$

Rotation curves of 12 subhalos with most massive progenitors

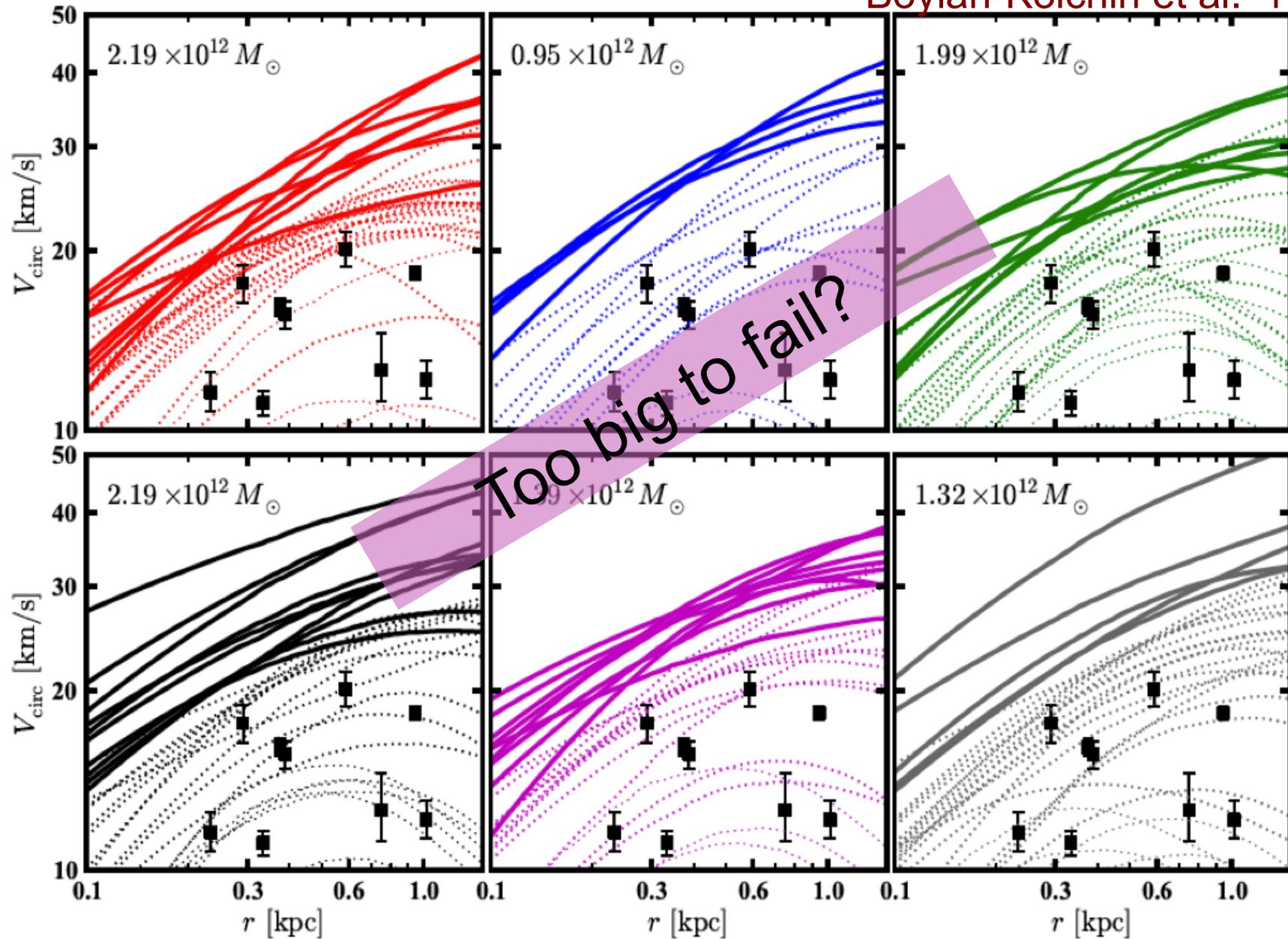
Red  $\rightarrow$  3 halos with most massive progenitors (LMC, SMC, Sagittarius?)

Lovell, Eke, Frenk, Gao et al '11;  
see also Boylan-Kolchin et al '11a,b



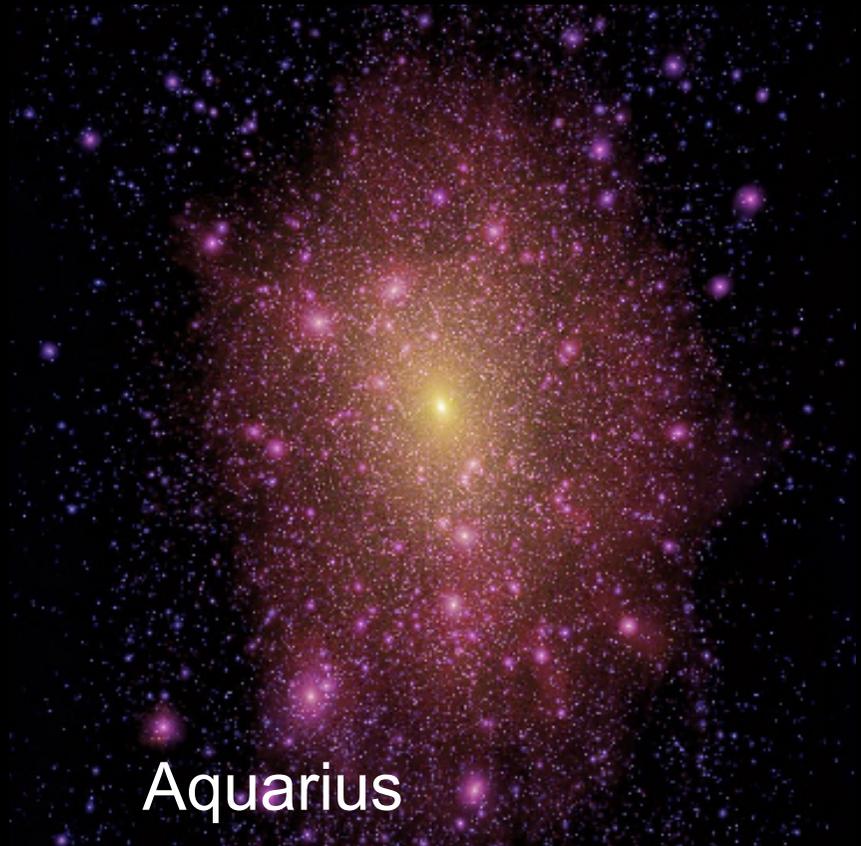
# Rotation curves of Aquarius subhalos

Boylan-Kolchin et al. '11

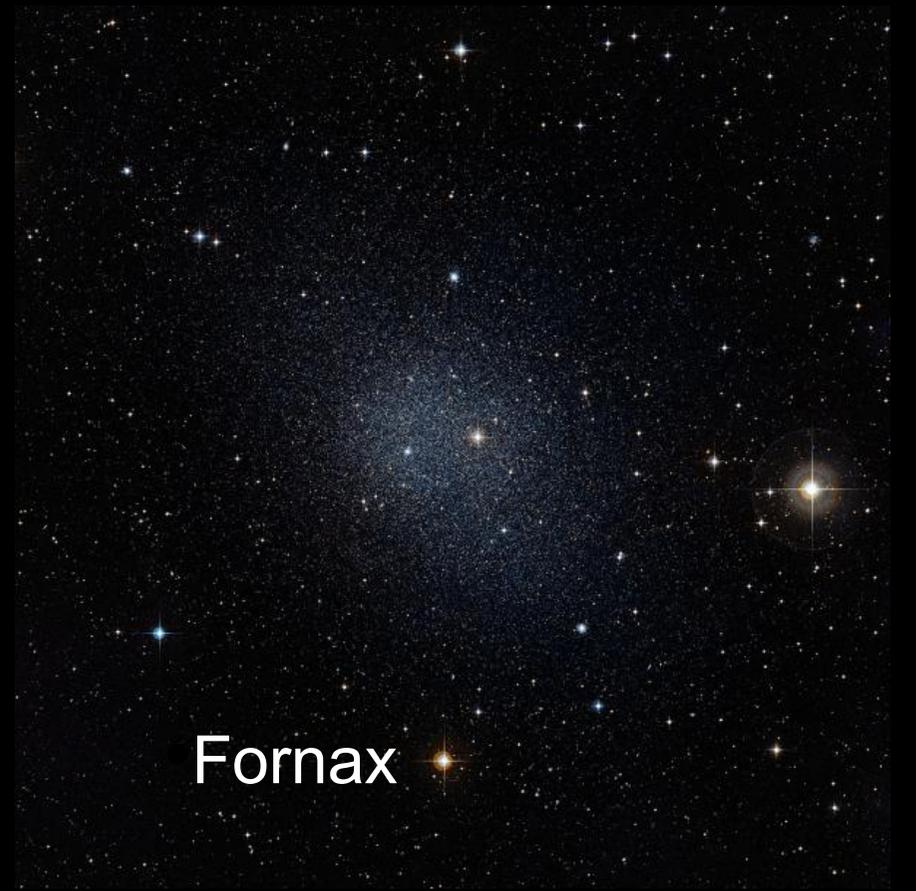




The Aquarius halos have  $\sim 10$  subhalos with too large a  $V_{\max}$  (i.e. much too concentrated) to be compatible with observed kinematics of MW dwarfs



Aquarius



Fornax



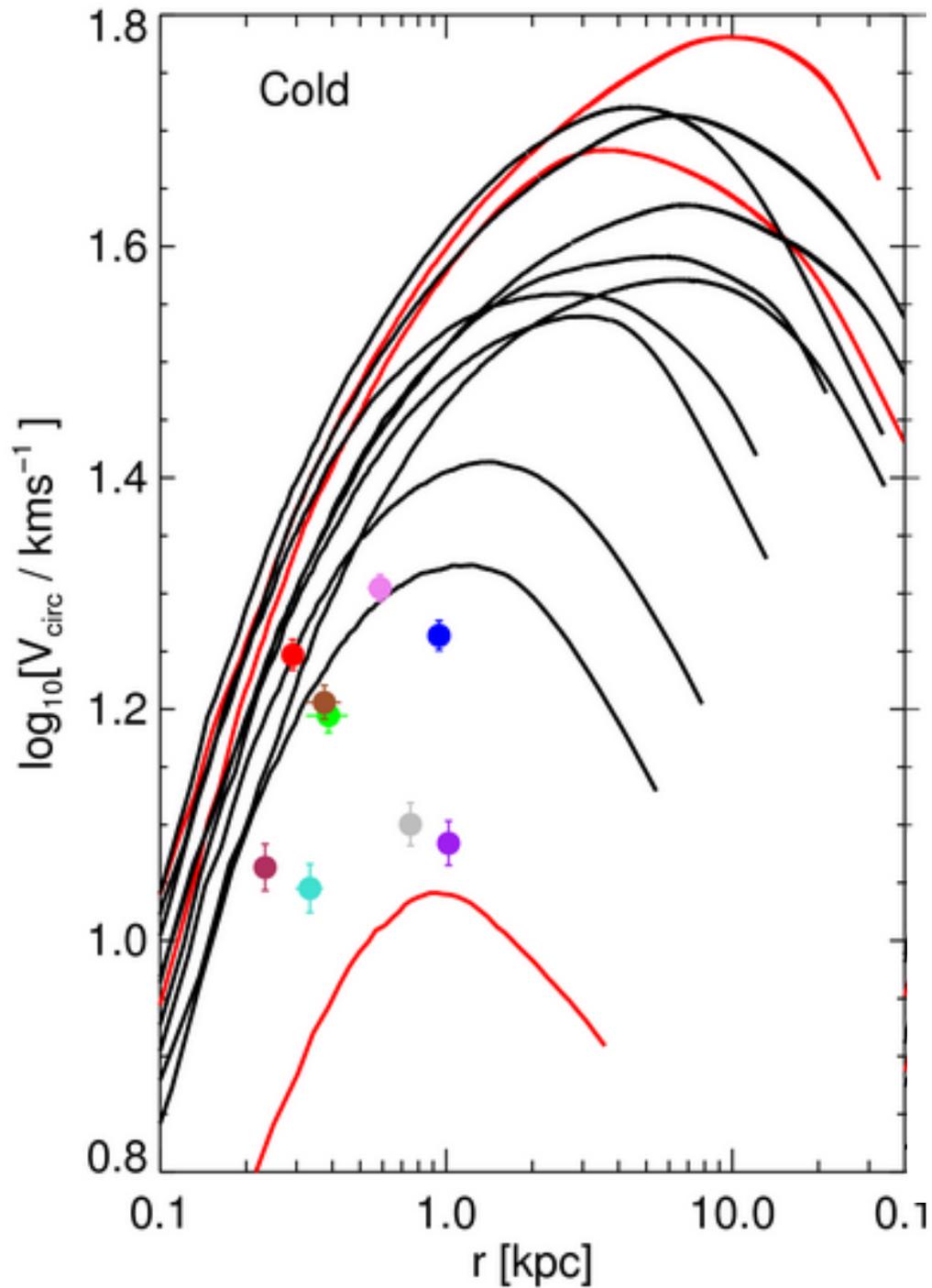
cold dark matter



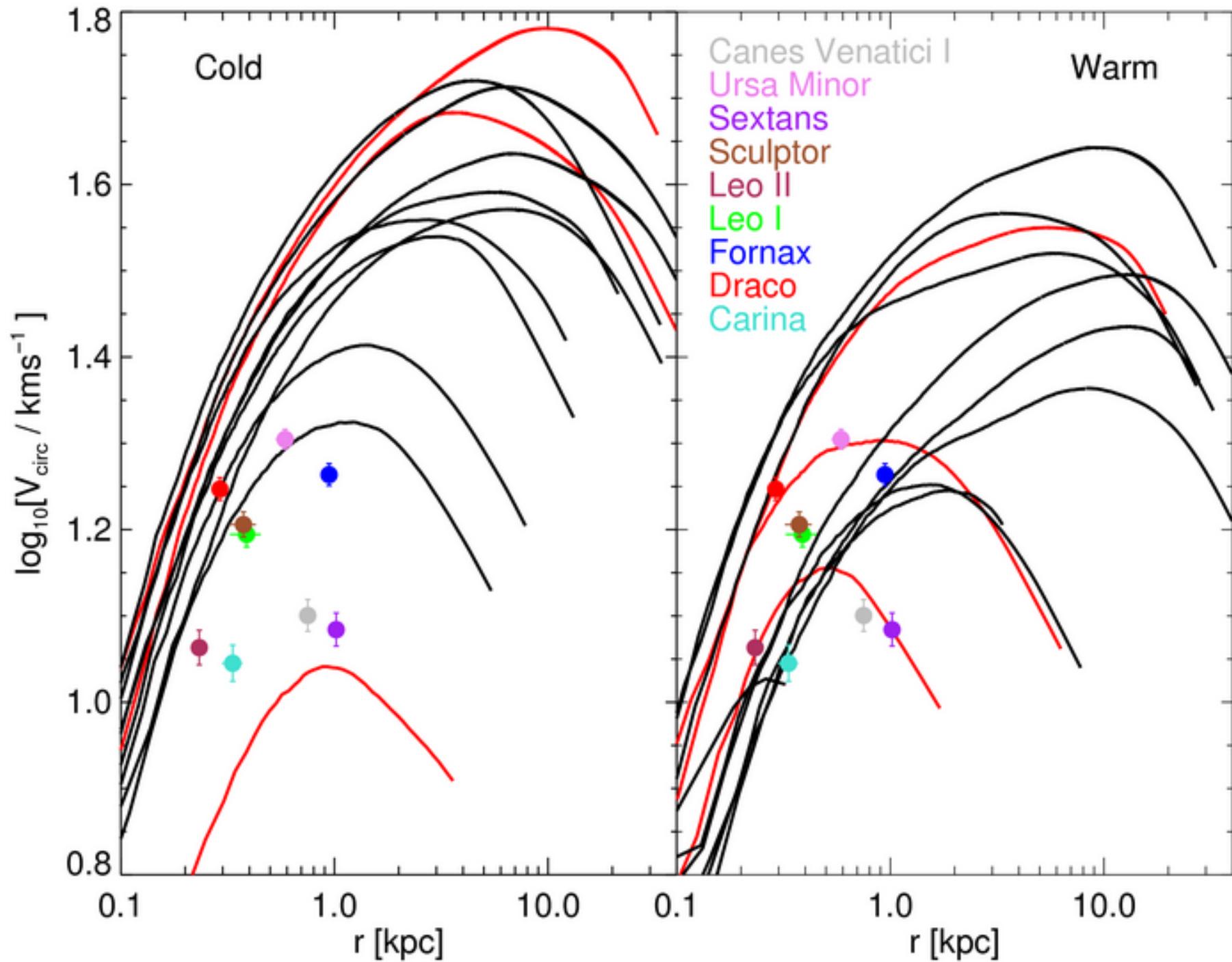
warm dark matter



Lovell, Eke, Frenk, Gao, Jenkins, Wang, White, Theuns,  
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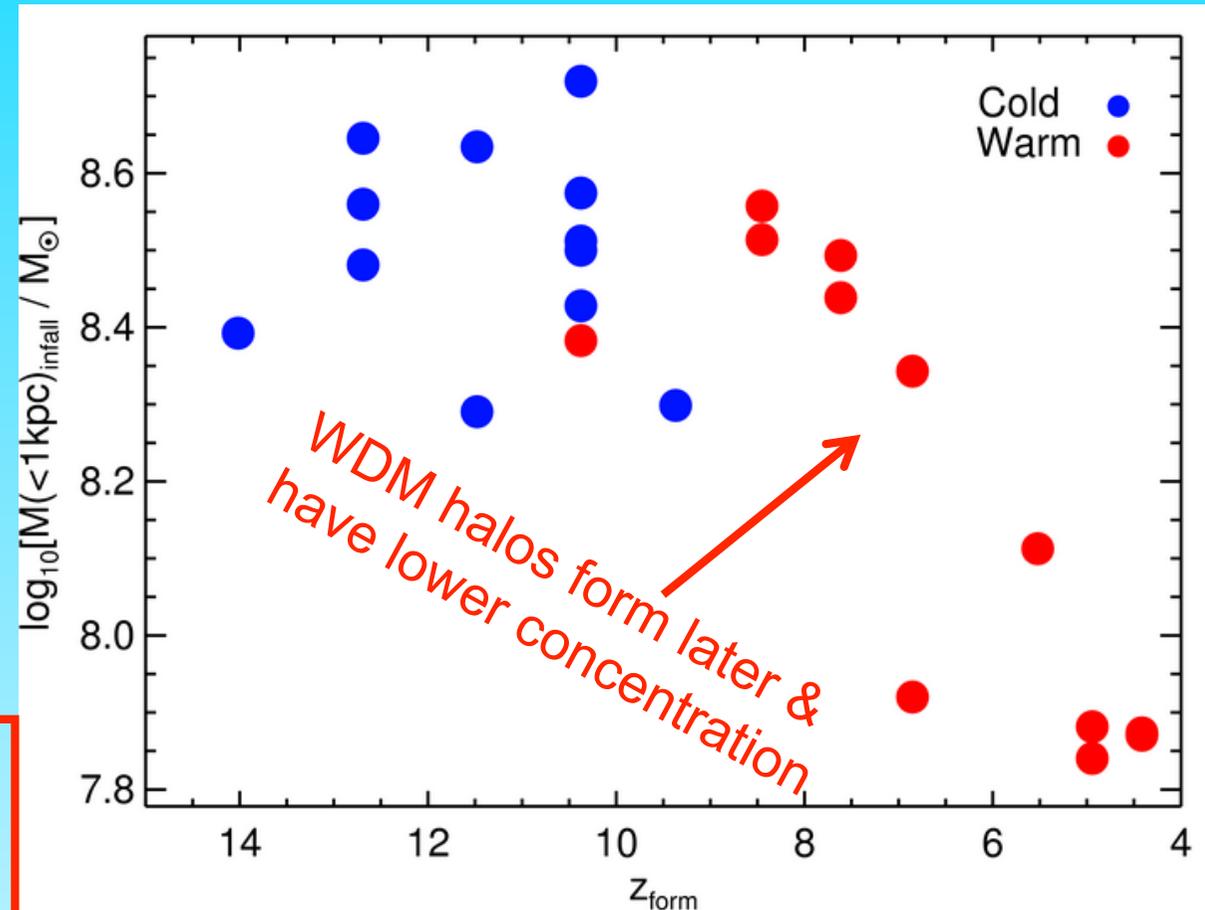
# Warm vs cold dark matter subhalos

“Formation redshift” →  
 $z$  at which  $M_{\text{halo}}$  first  
 exceeded  $M_{\text{infall}} (< 1 \text{ kpc})$

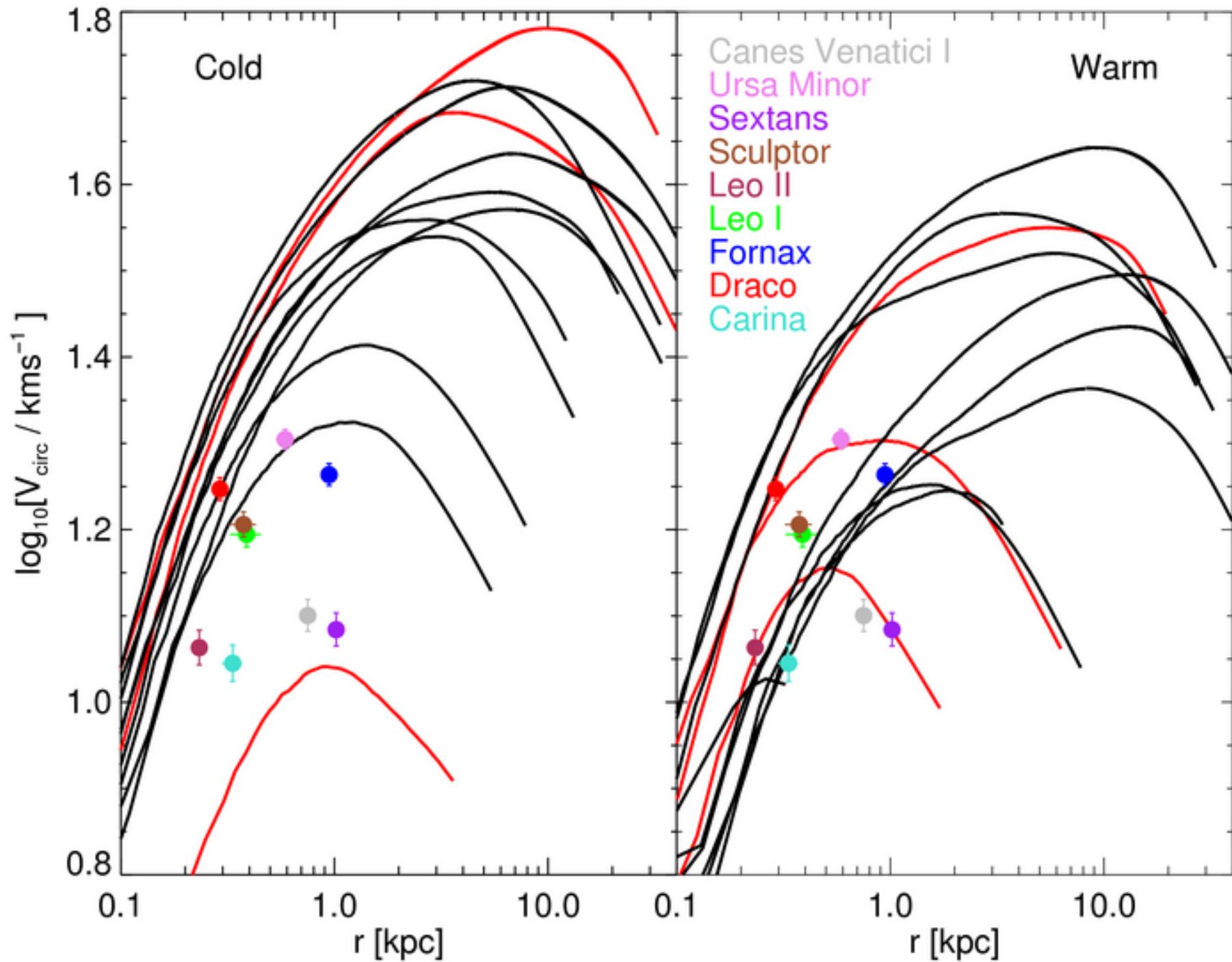
WDM halos form later  
 & have lower central  
 masses than their  
 CDM counterparts!



WDM subhalos are still  
 cuspy but are less  
 concentrated than CDM  
 subhalos



Lovell, Eke, Frenk, Gao, Jenkins et al '11





## Is this the end of CDM?

1. Baryon effects
2. The mass of the MW

## The cores of dwarf galaxy haloes

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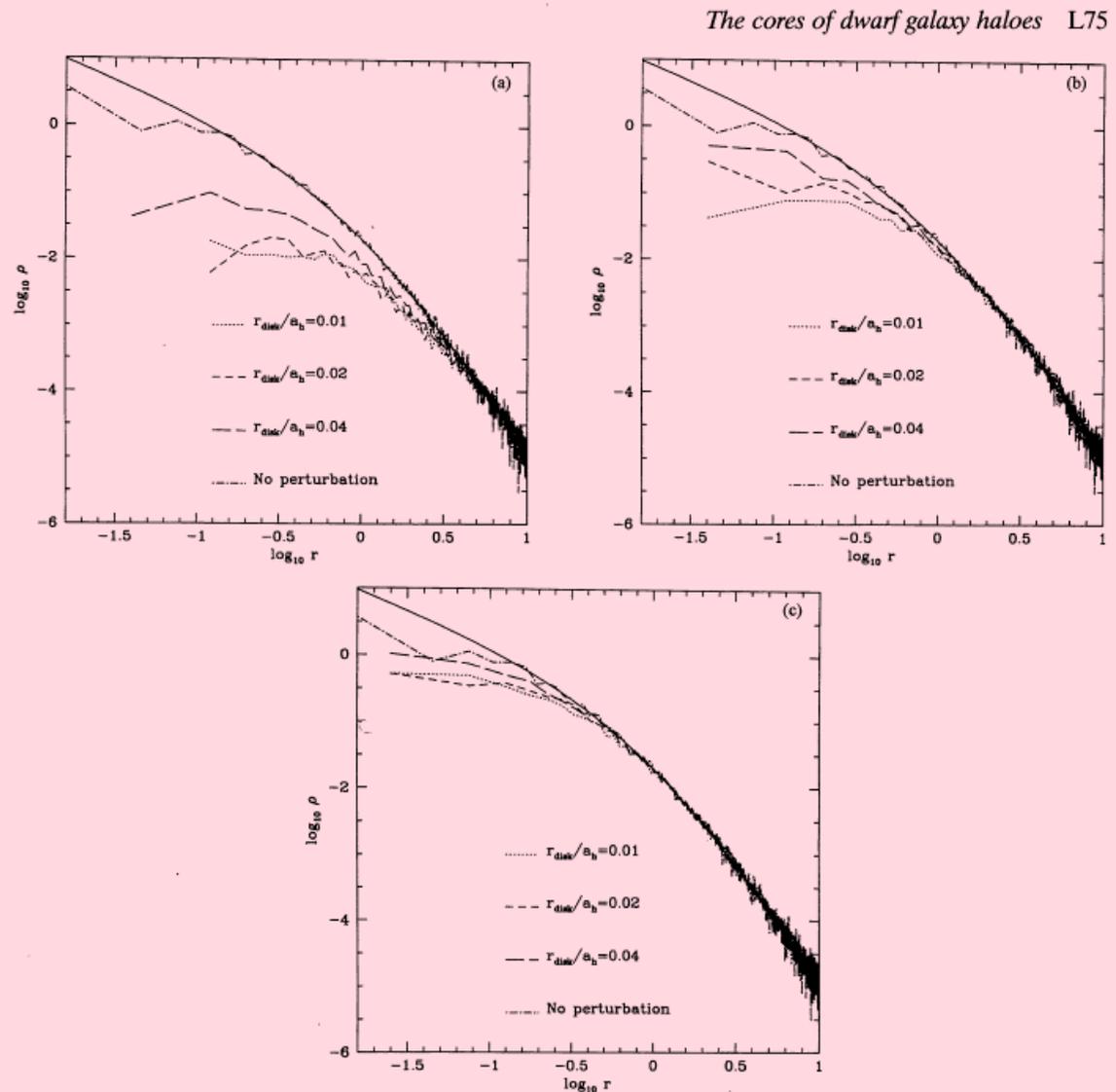
### ABSTRACT

We use  $N$ -body simulations to examine the effects of mass outflows on the density profiles of cold dark matter (CDM) haloes surrounding dwarf galaxies. In particular, we investigate the consequences of supernova-driven winds that expel a large fraction of the baryonic component from a dwarf galaxy disc after a vigorous episode of star formation. We show that this sudden loss of mass leads to the formation of a core in the dark matter density profile, although the original halo is modelled by a coreless (Hernquist) profile. The core radius thus created is a sensitive function of the mass and radius of the baryonic disc being blown up. The loss of a disc with mass and size consistent with primordial nucleosynthesis constraints and angular momentum considerations imprints a core radius that is only a small fraction of the original scalelength of the halo. These small perturbations are, however, enough to reconcile the rotation curves of dwarf irregulars with the density profiles of haloes formed in the standard CDM scenario.

Let baryons cool and condense to the galactic centre

Rapid ejection of large fraction of gas during starburst can lead to a core in the halo dark matter density profile

Navarro, Eke, Frenk '96  
Ponzen & Governato '12



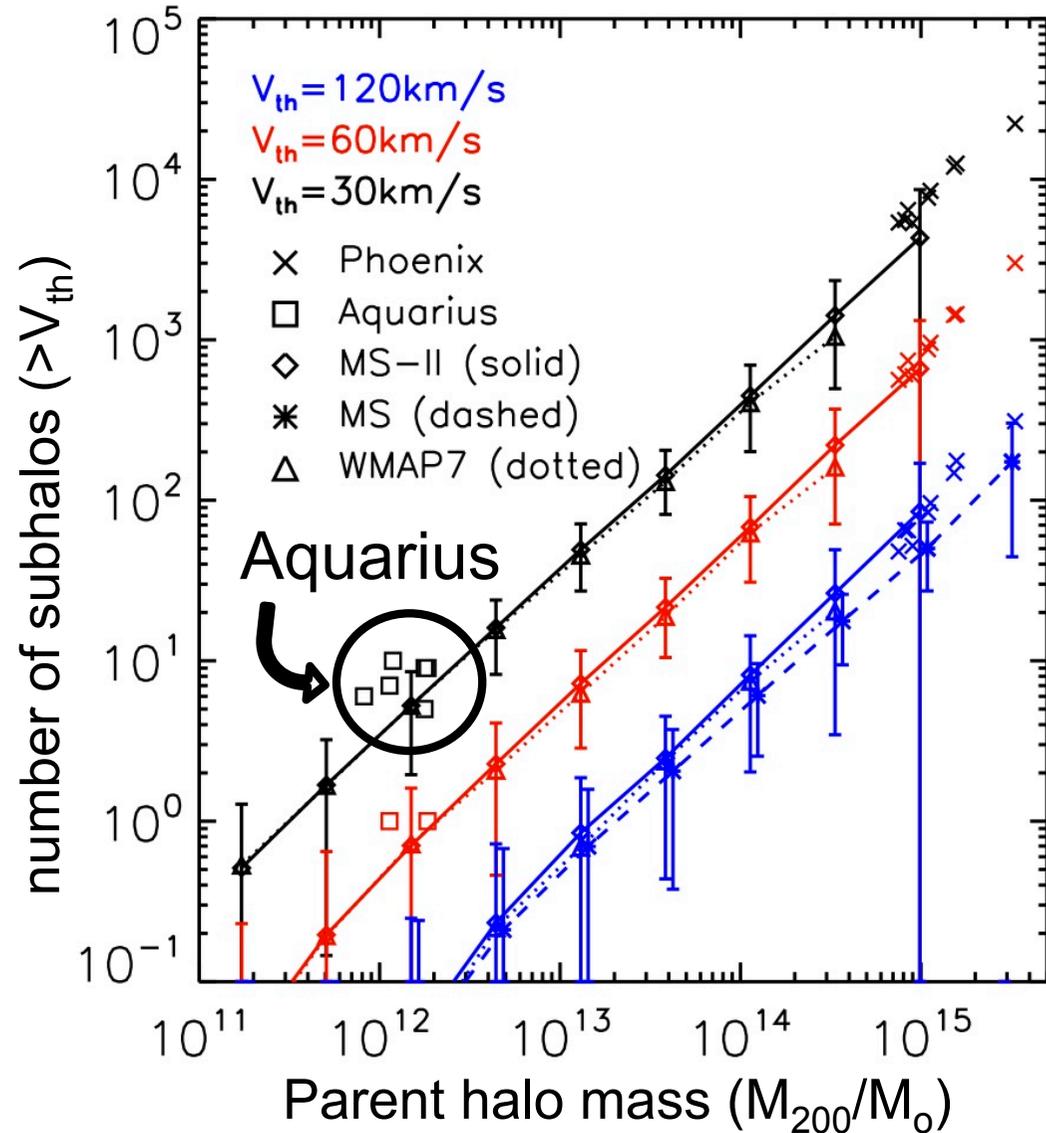
**Figure 3.** Equilibrium density profiles of haloes after removal of the disc. The solid line is the original Hernquist profile, common to all cases. The dot-dashed line is the equilibrium profile of the 10 000-particle realization of the Hernquist model run in isolation at  $t=200$ . (a)  $M_{\text{disc}}=0.2$ . (b)  $M_{\text{disc}}=0.1$ . (c)  $M_{\text{disc}}=0.05$ .

# Number of massive subhalos

Number of massive subhalos increases rapidly with halo mass

Aquarius halos have  $M \sim 2 \times 10^{12} M_{\odot}$

**But:** is this the mass of the MW halo?



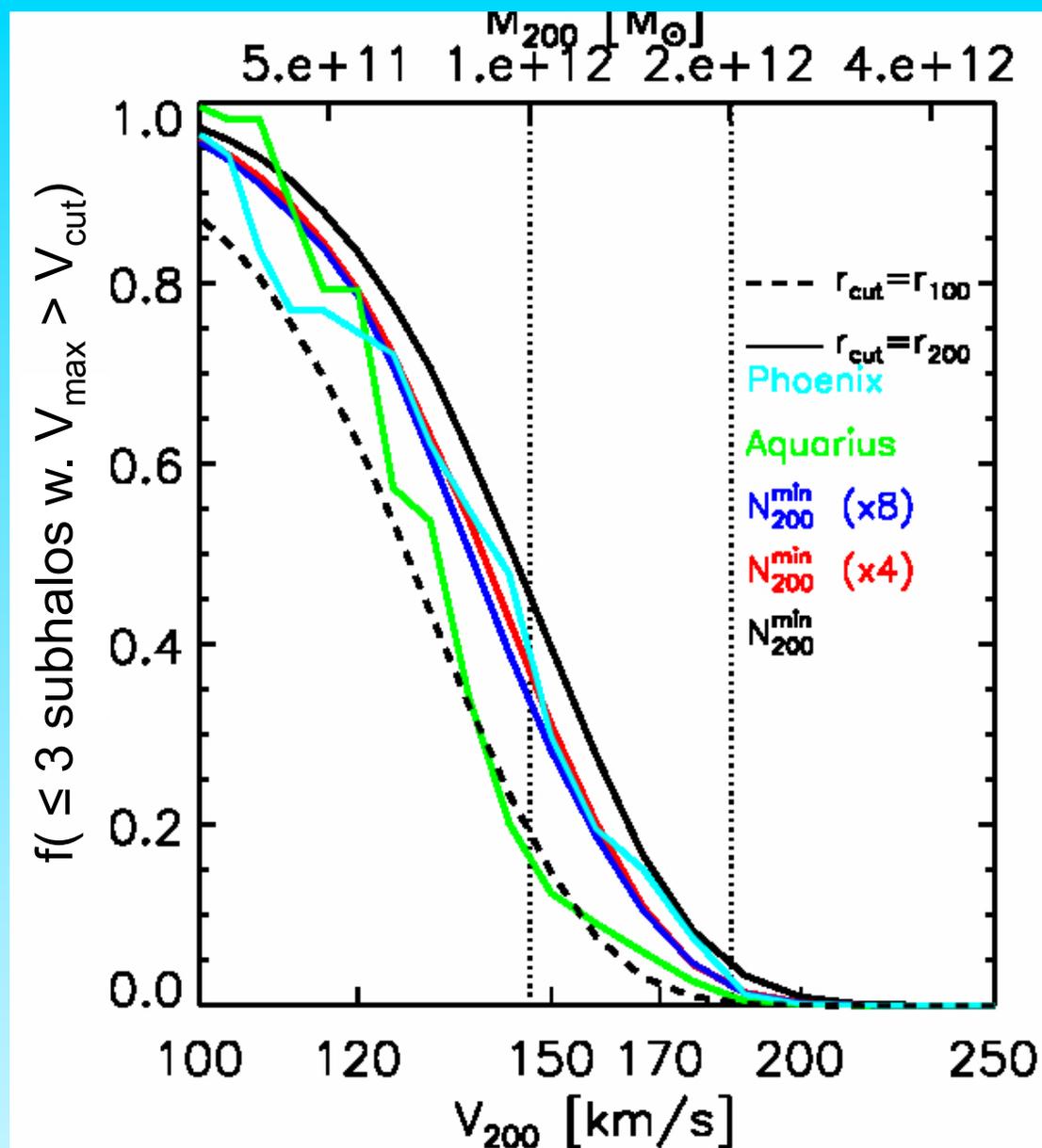
# Probability of massive subhalos

Probability of having no more than 3 subhalos with  $V_{\max} > 30 \text{ km/s}$

Depends strongly on  $M_{200}$  (and  $V_{\text{cut}}$ )

If mass of MW  $> 2 \times 10^{12} M_{\odot}$ ,  
CDM is ruled out!

If mass of MW  $\sim 1 \times 10^{12} M_{\odot}$ ,  
CDM is OK



## $\Lambda$ CDM: problems/possible solutions

- $\Lambda$ CDM great **success** on scales  $> 1\text{Mpc}$ : CMB, LSS, gal evolution

A problem on subgalactic scales?

Two NO-problems:

1. The satellite **LF**  $\rightarrow$  can be explained by **galaxy formation**
2. Central **cores**  $\rightarrow$  data **consistent** with **cusps**

However:

- CDM models place **brightest sats** in most massive subhalos and these appear to be **too concentrated** to be **compatible** w. **kinematics**

Possible solutions:

- Warm dark matter
- Baryon effects that make large CDM subhalos less concentrated
- Sat. pop. in the MW is very atypical or  $M_{\text{halo}} \leq 10^{12}M_{\odot}$

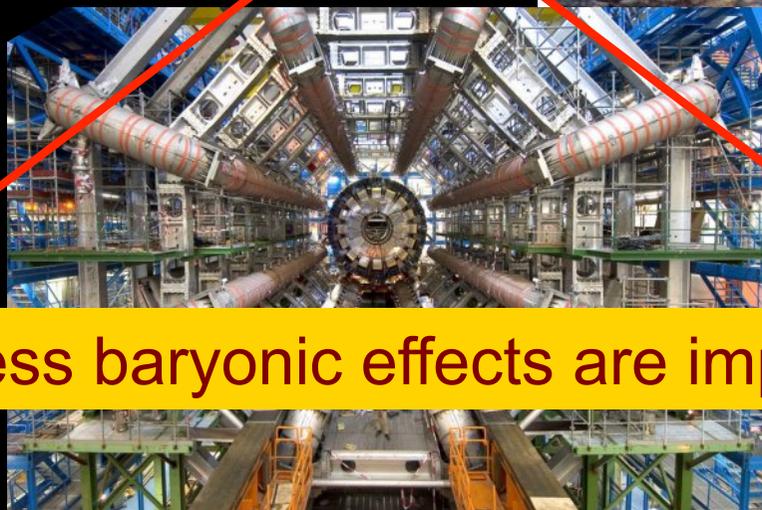
# Cold dark matter ?

If mass of MW halo  $> 2 \times 10^{12} M_{\odot}$

Fermi

Direct detection

Annihilation radiation



UK DM search  
(Boulby mine)

Unless baryonic effects are important

Evidence for SUSY

# Warm dark matter ?

Sterile neutrino detection possible

Decay line in X-rays



Constellation X

